# nag\_opt\_sparse\_mps\_read (e04mzc)

#### 1. Purpose

nag\_opt\_sparse\_mps\_read (e04mzc) reads data for a sparse linear programming or quadratic programming problem from a file which is in standard or compatible MPSX input format.

## 2. Specification

## 3. Description

nag\_opt\_sparse\_mps\_read reads linear programming (LP) or quadratic programming (QP) problem data from a file which is prepared in standard or compatible MPSX input format and then initializes n (the number of variables), m (the number of general linear constraints), the m by n matrix A, and the vectors l, u and c (stored in row **iobj** of A) for use with nag\_opt\_sparse\_convex\_qp (e04nkc), which is designed to solve problems of the form

$$\underset{x \in R^n}{\text{minimize}} \quad c^T x + \frac{1}{2} x^T H x \quad \text{subject to} \quad l \le \left\{ \begin{array}{c} x \\ Ax \end{array} \right\} \le u. \tag{1}$$

For LP problems, H=0. For QP problems, a function must be provided to nag\_opt\_sparse\_convex\_qp (e04nkc) to compute Hx for any given vector x. (This is illustrated in Section 6.) The optional parameter **minimize** may be used to specify whether the objective function is to be minimized or maximized. The document for nag\_opt\_sparse\_convex\_qp (e04nkc) should be consulted for further details.

Since, in general, the exact size of the problem defined by an MPSX file may not be known in advance, the arrays returned by nag\_opt\_sparse\_mps\_read are all allocated internally.

#### **MPSX Input Format**

The MPSX data file may only contain two types of line:

- (a) Indicator lines (specifying the type of data which is to follow).
- (b) Data lines (specifying the actual data).

The input file must not contain any blank lines. Any characters beyond column 80 are ignored. Indicator lines must not contain leading blank characters (in other words they must begin in column 1). The following displays the order in which the indicator lines must appear in the file:

```
NAME user-supplied name
ROWS
data line(s)

COLUMNS
data line(s)

RHS
data line(s)

RANGES (optional)
data line(s)

BOUNDS (optional)
data line(s)

ENDATA
```

The 'user-supplied name' specifies a name for the problem and must occupy columns 15–22. The name can either be blank or up to a maximum of 8 characters.

A data line follows the same fixed format made up of fields defined below. The contents of the fields may have different significance depending upon the section of data in which they appear.

	Field 1	Field 2	Field 3	Field 4	Field 5	Field 6
Columns	2-3	5 - 12	15 – 22	25 - 36	40 – 47	50 – 61
Contents	$\operatorname{Code}$	Name	Name	Value	Name	Value

The names and codes consist of 'alphanumeric' characters (i.e., a–z, A–Z, 0–9, +, -, asterisk (\*), blank ( ), colon (:), dollar sign (\$) or full stop (.) only) and the names must not contain leading blank characters. Values may be entered in several equivalent forms. For example, 1.2345678, 1.2345678e+0, 123.45678e-2 and 12345678E-07 all represent the same number. It is safest to include an explicit decimal point. Note that the lower case 'e' exponential notation is not standard MPSX, and if compatibility with other MPSX readers is required then the upper case notation should be used. The lower case notation is supported by nag\_opt\_sparse\_mps\_read since this is the natural notation in a C programming language environment.

It is recommended that numeric values be *right-justified* in the 12-character field, with no trailing blanks. This is to ensure compatibility with other MPSX readers, some of which may, in certain situations, interpret trailing blanks as zeros. This can dramatically affect the interpretation of the value and is relevant if the value contains an exponent, or if it contains neither an exponent nor an explicit decimal point.

Comment lines are allowed in the data file. These must have an asterisk (\*) in column 1 and any characters in columns 2–80. In any data line, a dollar sign (\$) as the first character in field 3 or 5 indicates that the information from that point through column 80 consists of comments.

Columns outside the six fields must be blank, except for columns 72–80, whose contents are ignored by the routine. These columns may be used to enter a sequence number. A non-blank character outside the predefined six fields and columns 72–80 is considered to be a major error unless it is part of a comment.

#### **ROWS Data Lines**

These lines specify row (constraint) names and their inequality types (i.e., =,  $\geq$  or  $\leq$ ).

Field 1: defines the constraint type as follows (may be in column 2 or column 3):

- M free row, i.e., no constraint. It may be used to define the objective row.
- G greater than or equal to (i.e.,  $\geq$ ).
- L greater than or equal to (i.e.,  $\leq$ ).
- E exactly equal to (i.e., =).

Field 2: defines the row name.

Row type N stands for 'Not binding', also known as 'Free'. It can be used to define the objective row. The objective row is a free row that specifies the vector c in the linear objective term  $c^Tx$ . It is taken to be the first free row, unless some other free row name is specified by the optional parameter **obj\_name** (see Section 7.2). Note that c is assumed to be zero if (for example) the line

## %N%%DUMMYROW

(where % denotes a blank) appears in the ROWS section of the MPSX data file, and the row name DUMMYROW is omitted from the COLUMNS section.

## **COLUMNS Data Lines**

These lines specify the names to be assigned to the variables (columns) in the general linear constraint matrix A, and define, in terms of column vectors, the actual values of the corresponding matrix elements.

- Field 1: blank (ignored).
- Field 2: gives the name of the column associated with the elements specified in the following fields.
- Field 3: contains the name of a row.

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- Field 4: used in conjunction with field 3; contains the value of the matrix element.
- Field 5: is optional (may be used like field 3).
- Field 6: is optional (may be used like field 4).

Note that only the non-zero elements of A and c need to be specified in the COLUMNS section, as any zero elements of A are removed and any unspecified elements of c are assumed to be zero. In addition, any non-zero elements in the jth column of A must be grouped together before those in the (j+1)th column, for  $j=1,2,\ldots,\mathbf{n}-1$ . Non-zero elements within a column may however appear in any order.

#### **RHS Data Lines**

This section specifies the right-hand side values of the general linear constraint matrix A (if any). The lines specify the name to be given to the right-hand side (RHS) vector along with the numerical values of the elements of the vector, which may appear in any order. The data lines have exactly the same format as the COLUMNS data lines, except that the column name is replaced by the RHS name. Only the non-zero elements need be specified. Note that this section may be empty, in which case the RHS vector is assumed to be zero.

### RANGES Data Lines (optional)

Ranges are used for constraints of the form  $l \leq Ax \leq u$ , where both l and u are finite. The effect of specifying a range  $r_j$  for constraint j depends on the type of the constraint (i.e., G, L or E), the sign of  $r_j$ , and the bound associated with the constraint in the RHS section. (Recall that this bound is taken to be zero if the constraint has no entry in the RHS section.) The various possibilities may be summarized as follows.

Row Type	Sign of $r_i$	Bound from RHS	Resultant $l_i$	Resultant $u_i$
G	+  or  -	$l_{j}$	$l_{i}$	$l_i +  r_i $
L	+ or -	$u_j$	$u_j -  r_j $	$u_{j}$
E	+	$l_j^{\circ}$	$l_j$	$l_j + r_j$
E	_	$u_j^{\cdot}$	$u_j -  r_j $	$u_{j}$

The data lines have exactly the same format as the COLUMNS data lines, except that the column name is replaced by the RANGE name.

#### **BOUNDS** Data Lines (optional)

These lines specify limits on the values of the variables (l and u in  $l \le x \le u$ ). If the variable is not specified in the bound set then it is automatically assumed to lie between default lower and upper bounds (usually 0 and  $+\infty$ ). (These default bounds may be reset to the values specified by the optional parameters **collo\_default** and **col\_up\_default**; see Section 7.2.) Like an RHS column which is given a name, the set of variables in one bound set is also given a name.

Field 1: specifies the type of bound or defines the variable type as follows:

- LO lower bound.
- UP upper bound.
- FX fixed variable.
- FR free variable  $(-\infty \text{ to } +\infty)$ .
- MI lower bound is  $-\infty$ .
- PL upper bound is  $+\infty$ . This is the default variable type.
- Field 2: identifies a name for the bound set.
- Field 3: identifies the column name of the variable belonging to this set.
- Field 4: identifies the value of the bound; this has a numerical value only in association with LO, UP, FX in field 1, otherwise it is blank.
- Field 5: is blank and ignored.

Field 6: is blank and ignored.

Note that if RANGES and BOUNDS sections are both present, the RANGES section must appear first.

#### MPSX and Integer Programming Problems

The MPSX input format allows the specification of *integer programming* (IP) problems in which some or all of the variables are constrained to take integer values within a specified range. nag\_opt\_sparse\_mps\_read can read MPSX files defining IP problems in either the 'compatible' or 'standard' formats. However, any integer restrictions are ignored: any variable upon which such restrictions are defined by the file is simply treated as a continuous variable with upper and lower bounds as specified. The facility to read such files is offered to allow users to solve IP problems in their 'relaxed' LP or QP form using nag\_opt\_sparse\_convex\_qp (e04nkc). The compatible and standard MPSX forms are described below. Users not interested in this facility may skip the remainder of this section.

In the compatible MPSX format, the type of integer variables are defined in Field 1 of the BOUNDS section, that is:

Field 1: specifies the type of the integer variable as follows:

BV 0-1 integer variable (bound value is 1.0).

UI general integer variable (bound value is in field 4).

In the standard MPSX format, the integer variables are treated the same as 'ordinary' bounded variables, in the BOUNDS section. Integer markers are, however, introduced in the COLUMNS section to specify the integer variables. The indicator lines for these markers are:

	Field 1	Field 2	Field 3	Field 4	Field 5	Field 6
Columns	2-3	5 - 12	15 – 22	25 - 36	40 – 47	50 – 61
Contents		name	'MARKER'		'INTORG'	
to mark the begi	inning of the	e integer va	riables and			
	Field 1	Field 2	Field 3	Field 4	Field 5	Field 6
Columns	2-3	5 - 12	15 - 22	25 - 36	40 – 47	50 – 61
Contents		name	'MARKER'		'INTEND'	

to mark the end. That is, any variables between these markers are treated as integer variables. The *name* in Field 2 may be any name different from the preceding and following column names, the other entries in the indicator lines must be exactly as described above (including quotation marks). Note that if the INTEND indicator line is not specified then all columns between the INTORG indicator line and the end of the COLUMNS section are assumed to be integer variables. nag\_opt\_sparse\_mps\_read accepts both standard and/or compatible MPSX format as a means of specifying integer variables.

## 4. Parameters

## mps\_file

 $\mathbf{m}$ 

Input: the name of the MPSX data file. If **mps\_file** is a null pointer or null string, then the data is assumed to come from **stdin**.

Output: the number of columns (variables) specified by the data file.

Output: the number of rows specified by the data file. This is the number of general linear constraints in the problem, including the objective row.

nnz
Output: the number of non-zeros in the problem (including the objective row).

**iobj** Output: if **iobj** > 0, row **iobj** of A is a free row containing the non-zero coefficients of the vector c (the rows of A are indexed  $1, 2, \ldots, \mathbf{m}$ ). If **iobj** = 0, the coefficients of c are assumed to be zero.

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a

Output: the nnz non-zero elements of A, ordered by increasing column index.

Sufficient memory is allocated internally by nag\_opt\_sparse\_mps\_read and may be freed by the utility function nag\_opt\_sparse\_mps\_free (e04myc).

ha

Output: the  $\mathbf{nnz}$  row indices of the non-zero elements of A.

Sufficient memory is allocated internally by nag\_opt\_sparse\_mps\_read and may be freed by the utility function nag\_opt\_sparse\_mps\_free (e04myc).

ka

Output: the  $\mathbf{n}+1$  indices indicating the beginning of each column of A in  $\mathbf{a}$ . More precisely,  $\mathbf{ka}[j-1]$  contains the index in  $\mathbf{a}$  of the start of the jth column, for  $j=1,2,\ldots,\mathbf{n}-1$ . Note that  $\mathbf{ka}[0]=0$  and  $\mathbf{ka}[\mathbf{n}]=\mathbf{nnz}$ .

Sufficient memory is allocated internally by nag\_opt\_sparse\_mps\_read and may be freed by the utility function nag\_opt\_sparse\_mps\_free (e04myc).

bl bu

Output: **bl** and **bu** hold the lower bounds and upper bounds, respectively, for all the variables and constraints, in the following order. The first **n** elements contain the bounds on the variables x and the next **m** elements contain the bounds for the linear objective term  $c^Tx$  and the general linear constraints Ax (if any). Note that an 'infinite' lower bound is indicated by  $\mathbf{bl}[j-1] = -10^{20}$ , an 'infinite' upper bound by  $\mathbf{bl}[j-1] = 10^{20}$ , and an equality constraint by  $\mathbf{bl}[j-1] = \mathbf{bu}[j-1]$ . (The lower bound for  $c^Tx$ , stored in  $\mathbf{bl}[\mathbf{n+iobj}-1]$ , is set to **-options.col\_up\_default**, and the upper bound, stored in  $\mathbf{bl}[\mathbf{n+iobj}-1]$  is set to **options.col\_up\_default**; the optional parameter **col\_lo\_default** has a default value of  $10^{20}$ ; see Section 7.)

Sufficient memory is allocated internally by nag\_opt\_sparse\_mps\_read and may be freed by the utility function nag\_opt\_sparse\_mps\_free (e04myc).

XS

Output: a set of initial values for the **n** variables and **m** constraints in the problem. More precisely,  $\mathbf{xs}[j] = \min(\max(0.0, \mathbf{bl}[j]), \mathbf{bu}[j])$ , for  $j = 0, 1, \dots, \mathbf{m+n-1}$ .

Sufficient memory is allocated internally by nag\_opt\_sparse\_mps\_read and may be freed by the utility function nag\_opt\_sparse\_mps\_free (e04myc).

## options

Input/Output: a pointer to a structure of type Nag\_E04\_Opt whose members are optional parameters for nag\_opt\_sparse\_mps\_read. These structure members offer the means of adjusting the parameter values used when reading in the MPSX file and on output will supply further details of the results. A description of the members of **options** is given below in Section 7.2.

If any of these optional parameters are required then the structure **options** should be declared and initialized by a call to nag\_opt\_init (e04xxc) and supplied as an argument to nag\_opt\_sparse\_mps\_read. However, if the optional parameters are not required the NAG defined null pointer, E04\_DEFAULT, can be used in the function call.

fail

The NAG error parameter, see the Essential Introduction to the NAG C Library. Users are recommended to declare and initialize **fail** and set **fail.print** = **TRUE** for this function.

#### 4.1. Description of Printed Output

Results are printed out by default. The level of printed output can be controlled by the user with the structure members **options.list** and **options.output\_level** (see Section 7.2). If **list** = **TRUE** then the parameter values to nag\_opt\_sparse\_mps\_read are listed, whereas the printout of results is governed by **output\_level**. The default print level of **Nag\_MPS\_Summary** gives the following information if the MPSX file has been read successfully:

- (a) the number of lines read.
- (b) the number of columns specified by the data. If any of these are specified as integer variables, the number of such variables is also reported. (However, recall that nag\_opt\_sparse\_mps\_read will nevertheless regard such variables as continuous variables; see Section 3).
- (c) the number of rows specified by the data. The objective row is counted amongst these.

In addition, the names of the problem, the objective row, the RHS set, the RANGES set, and the BOUNDS set read are listed. Unless specified otherwise by the optional parameters **prob\_name**, **obj\_name**, **rhs\_name**, **range\_name** and/or **bnd\_name** (see Section 7), these names will correspond to the first problem, objective row, etc., encountered in the MPSX file. Where no set was encountered (RANGES and BOUNDS are optional), a 'blank' is output.

Additionally, when **output\_level** = **Nag\_MPS\_List**, each line of the MPSX file is echoed as it is read. This may be useful as a debugging aid.

If **output\_level** = **Nag\_MPS\_NoOutput** then printout will be suppressed; the user can print the information contained in (b) and (c) when nag\_opt\_sparse\_mps\_read returns to the calling program.

#### 5. Comments

A list of possible error exits and warnings from nag\_opt\_sparse\_mps\_read is given in Section 8.

#### 6. Example 1

To solve the quadratic programming problem

$$\begin{array}{ll} \text{minimize} & c^Tx + \frac{1}{2}x^THx \\ \text{subject to} & l & \leq Ax \leq & u, \\ -2 & \leq & x \leq & 2, \end{array}$$

where

$$A = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 4 \\ 1 & 2 & 3 & 4 & -2 & 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & 1 & -1 & 1 & 1 & 1 & 1 \end{pmatrix}, \quad l = \begin{pmatrix} -2 \\ -2 \\ -2 \end{pmatrix} \quad \text{and} \quad u = \begin{pmatrix} 1.5 \\ 1.5 \\ 4.0 \end{pmatrix}.$$

The optimal solution (to five significant figures) is

$$x^* = (2.0, -0.23333, -0.26667, -0.3, -0.1, 2.0, 2.0, -1.7777, -0.45555)^T$$
.

Three bound constraints and two general linear constraints are active at the solution. Note that, although the Hessian is positive semi-definite, the point  $x^*$  is the unique solution.

This example shows the simple use of nag\_opt\_sparse\_mps\_read where default values are used for all parameters, in conjunction with nag\_opt\_sparse\_convex\_qp (e04nkc). An example showing the use of the optional parameters is given in Section 12. There is one example program file, the main program of which calls both examples. The C functions for the main program and Example 1

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are given below. The function to calculate Hx (required by nag\_opt\_sparse\_convex\_qp (e04nkc)) is qphess for this example.

Note the use of nag\_opt\_sparse\_mps\_free (e04myc) in this example to free the memory returned by nag\_opt\_sparse\_mps\_read, once the problem has been solved.

The MPSX representation of the problem is given in Section 6.2.

#### 6.1. Program Text

```
/* nag_opt_sparse_mps_read(e04mzc) Example Program.
 * Copyright 1998 Numerical Algorithms Group.
 * Mark 5, 1998.
 */
#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nag_string.h>
#include <nage04.h>
#ifdef NAG_PROTO
static void qphess(Integer ncolh, double x[], double hx[], Nag_Comm *comm);
static void ex1(void);
static void ex2(void);
static void qphess();
static void ex1();
static void ex2();
#endif
main()
  /* Two examples are called: ex1() uses the
   * default settings to read an MPSX file and
   * solve the problem, while ex2() uses the
   * options structure to obtain the column
   * and row names.
  Vprintf("e04mzc Example Program Results.\n");
  ex1();
  ex2();
  exit(EXIT_SUCCESS);
#ifdef NAG_PROTO
static void ex1(void)
#else
static void ex1()
#endif
  Integer iobj, m, n, ncolh, nnz;
  Integer ninf;
  Integer *ha, *ka;
  double *bl, *bu, *a, *xs;
  double obj, sinf;
  static NagError fail;
  Vprintf("\nExample 1: default options used.\n");
  fail.print = TRUE;
  /* Read the MPSX file */
  e04mzc((char*)0, &n, &m, &nnz, &iobj, &a, &ha, &ka, &bl, &bu, &xs,
         E04_DEFAULT, &fail);
  if (fail.code == NE_NOERROR)
```

```
{
           /* Solve the problem */
          ncolh = 5;
           }
       /* Free the memory allocated by e04mzc */
      e04myc(&a, &ha, &ka, &bl, &bu, &xs);
     #ifdef NAG_PROTO
     static void qphess(Integer ncolh, double x[], double hx[], Nag_Comm *comm)
     static void qphess(ncolh, x, hx, comm)
          Integer ncolh;
          double x[], hx[];
          Nag_Comm *comm;
     #endif
       /* Function to compute H*x. */
      hx[0] = 2.0*x[0] + x[1] + x[2] + x[3] + x[4];

hx[1] = x[0] + 2.0*x[1] + x[2] + x[3] + x[4];
      hx[2] = x[0] + x[1] + 2.0*x[2] + x[3] + x[4];
      hx[3] = x[0] + x[1] + x[2] + 2.0*x[3] + x[4];
      hx[4] = x[0] + x[1] + x[2] + x[3] + 2.0*x[4];
     } /* qphess */
     /* Example 2 */
6.2. Program Data
     * e04mzc Example Program Data
     * Example 1 MPSX data
     NAME
     ROWS
     L R1.....
     L R2.....
     L R3.....
N Free Row
     COLUMNS
                                         R2.....
        X1.... R1.... 1.0
X1.... R3.... 1.0
X2... R1 1.0
                                                             1.0
        X1....R3....
X2....R1....
X2....R3....
                                           Free Row
                                                             -4.0
                                 1.0
                                            R2....
                                                             2.0
                                           r∠...
Free Row
                               -1.0
                                                             -1.0
         X3..... R1.....
                                1.0
                                           R2....
                                                             3.0
        X3....R3.....
X4....R1.....
X4....R3.....
                                           Free Row
                                1.0
                                                             -1.0
                                           R2.....
Free Row
                                 1.0
                                                             4.0
                               -1.0
                                                             -1.0
                            1.0
         X5..... R1.....
                                           R2.....
                                                             -2.0
        X5.... R3....
X6.... R1....
X6.... R3....
X7.... R1....
                                           Free Row
                                                             -1.0
                               1.0
                                            R2.....
                                                             1.0
                                                             -1.0
                                 1.0
                                            Free Row
                                            R2.....
                                1.0
                                                             1.0
                               1.0
         X7..... R3.....
                                           Free Row
                                                             -1.0
         X8..... R1.....
                                 1.0
                                           R2.....
                                                             1.0
        X8..... R3.....
X9..... R1.....
                                            Free Row R2.....
                                 1.0
                                                             -0.1
                                 4.0
                                                             1.0
         X9..... R3.....
                                            Free Row
                                 1.0
                                                             -0.3
     RHS
         RHS1
                   R1....
                                 1.5
         RHS1
                   R2....
                                 1.5
                   R3.....
                                 4.0
         RHS1
     RANGES
         RANGE1
                                 3.5
                   R1.....
         RANGE1
                   R2....
                                 3.5
```

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6.3.

RANGE1 BOUNDS LO BOUND UP BOUND	X1 X2 X3 X4 X5 X6 X7 X8 X9 X1 X2 X3 X4 X5 X6 X7 X8 X6 X7 X8 X8 X8 X7 X8	6.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2			
Program Resu	lts				
e04mzc Examp	le Program Resul	ts.			
Example 1: d	efault options u	ised.			
Parameters t					
<pre>ncol_approx. est_density. output_level</pre>	(f(f0.05.0		rhs_namebnd_namecol_up_defaultnrow_approx	(first) (first) 1.00e+20 500	
MPS file suc Number of li Number of co Number of ro	lumns:	57 9 4 (in	cluding objective row)		
MPS Names Selected: Problem QP Objective Free Row RHS RHS1 RANGES RANGE1 BOUNDS BOUND					
MPS data successfully assigned to problem data.					
Parameters to e04nkc					
Linear const	spar	rse QP 4	Number of variables Hessian columns	9 5	
prob_name obj_name range_name crnames		plied	rhs_namebnd_name		
fcheck scale optim_tol		60 aScale 00e-06	start reset_ftol. factor_freq. scale_tol. max_iter. crash_tol.	10000 100 9.00e-01 65	

```
10
partial_price.....
                                   pivot_tol..... 2.04e-11
lu_update_tol..... 1.00e+01
lu_factor_tol..... 1.00e+02
lu_sing_tol..... 2.04e-11
                                   machine precision..... 1.11e-16
print_level......Nag_Soln_Iter
outfile..... stdout
Memory allocation:
state.....
                            Nag
                                   lambda.....
                                                               Nag
                 Ninf
                        Sinf/Objective
                                        Norm rg
   Itn
           Step
        0.0e + 00
                    0
                          0.000000e+00
                                        0.0e + 00
Itn
         0 -- Factorize detected a singular Hessian.
              Rank = 5, Diag, min diag = 0.0e+00, 3.3e-13.
        0.0e+00
                    0
                          0.000000e+00
                                        6.3e + 00
Itn 0 -- Feasible QP solution.
        7.5e-01
                         -4.375000e+00
                    0
                                        3.5e-01
    1
    2
        1.0e+00
                    0
                         -4.400000e+00
                                        0.0e+00
        1.9e-01
                         -4.700000e+00
    3
                    0
                                        1.6e+00
    4
        1.0e+00
                    0
                         -5.100000e+00
                                        2.2e-16
Itn
         5 -- Hessian numerically indefinite.
              Square of diag, min diag =
                                        -1.4e-14,
                                                    2.7e-13.
    5
        2.2e-01
                    0
                         -5.932500e+00
                                        3.7e+00
                                        1.1e+00
    6
        4.7e-01
                    0
                         -6.179688e+00
    7
        1.0e+00
                    0
                         -6.267162e+00
                                         2.2e-16
        8.1e-03
    8
                                        1.4e+00
                    Ω
                         -6.532489e+00
    9
        6.3e-01
                         -7.583236e+00
                                         1.3e-15
        1.0e+00
    10
                    0
                         -8.067718e+00
                                        8.9e-16
   11
        1.0e+00
                    0
                         -8.067778e+00
                                        2.2e-16
                                         Upper Bound
Variable State
                             Lower Bound
                                                       Lagr Mult
                                                                   Residual
                     Value
           UL
                2.00000e+00
                             -2.0000e+00
                                           2.0000e+00
                                                      -8.000e-01
                                                                  0.000e+00
X1....
X2....
          SBS
               -2.33333e-01
                             -2.0000e+00
                                          2.0000e+00
                                                       0.000e+00
                                                                  1.767e+00
ХЗ.....
          SBS
              -2.66667e-01
                             -2.0000e+00
                                           2.0000e+00
                                                       0.000e+00
                                                                  1.733e+00
                             -2.0000e+00
                                                                  1.700e+00
X4....
               -3.00000e-01
                                          2.0000e+00
                                                       0.000e+00
           BS
X5....
          SBS
               -1.00000e-01
                             -2.0000e+00
                                           2.0000e+00
                                                      -1.570e-16
                                                                  1.900e+00
                2.00000e+00
                             -2.0000e+00
                                          2.0000e+00
                                                      -9.000e-01
                                                                  0.000e + 00
X6.....
           UT.
X7....
           UL
                2.00000e+00
                             -2.0000e+00
                                           2.0000e+00
                                                      -9.000e-01
                                                                  0.000e+00
Х8.....
          SBS
               -1.77778e+00
                             -2.0000e+00
                                          2.0000e+00
                                                       1.761e-17
                                                                  2.222e-01
Х9.....
           BS
               -4.55556e-01
                             -2.0000e+00
                                          2.0000e+00
                                                      -5.551e-17
                                                                  1.544e+00
Constrnt State
                             Lower Bound
                                         Upper Bound
                     Value
                                                       Lagr Mult
                                                                   Residual
           UL
                1.50000e+00
                             -2.0000e+00
                                          1.5000e+00
                                                      -6.667e-02
                                                                  0.000e+00
R1....
                             -2.0000e+00
                                                                  0.000e+00
R2....
           UI.
                1.50000e+00
                                          1.5000e+00
                                                      -3.333e-02
R3.....
           BS
                3.93333e+00
                             -2.0000e+00
                                          4.0000e+00
                                                       0.000e+00
                                                                 -6.667e-02
Free Row
           BS
               -1.07856e+01
                                                      -1.000e+00
                                                                 -1.079e+01
                                    None
                                                None
Exit after 11 iterations.
```

Optimal QP solution found.

Final QP objective value = -8.0677778e+00

## 7. Optional Parameters

A number of optional input and output parameters to nag\_opt\_sparse\_mps\_read are available through the structure argument **options**, type Nag\_E04\_Opt. A parameter may be selected by assigning an appropriate value to the relevant structure member; those parameters not selected will be assigned default values. If no use is to be made of any of the optional parameters the user should use the NAG defined null pointer, E04\_DEFAULT, in place of **options** when calling nag\_opt\_sparse\_mps\_read; the default settings will then be used for all parameters.

Before assigning values to **options** directly the structure **must** be initialized by a call to the function nag\_opt\_init (e04xxc). Values may then be assigned to the structure members in the normal C manner.

Option settings may also be read from a text file using the function nag\_opt\_read (e04xyc) in which

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case initialization of the **options** structure will be performed automatically if not already done. Any subsequent direct assignment to the **options** structure must **not** be preceded by initialization.

#### 7.1. Optional Parameter Checklist and Default Values

For easy reference, the following list shows the members of **options** which are valid for nag\_opt\_sparse\_mps\_read together with their default values where relevant.

TRUE
Nag_MPS_Summary
stdout
'\0'
'\0'
'\0'
'\0'
'\0'
0.0
$10^{20}$
500
500
0.05
size $\mathbf{n}+\mathbf{m}$

### 7.2. Description of Optional Parameters

list - Boolean Default = TRUE

Input: if options.list = TRUE the parameter settings in the call to nag\_opt\_sparse\_mps\_read will be printed.

#### output\_level - Nag\_OutputType

Default = Nag\_MPS\_Summary

Input: the level of printout produced by nag\_opt\_sparse\_mps\_read. The following values are available.

Nag\_NoOutput No output.

Nag\_MPS\_Summary A summary of the dimensions of the problem read and a list of the

'MPSX names' (problem name, objective row name, etc.).

Nag\_MPS\_List As Nag\_MPS\_Summary but each line of the MPSX file is echoed

as it is read. This can be useful for debugging the file.

 $\label{level-level-level-nag-NoOutput} Constraint: \ options.output\_level = Nag\_NoOutput, \ Nag\_MPS\_Summary \ {\it or} \ Nag\_MPS\_List.$ 

```
outfile - char[80] Default = stdout
```

Input: the name of the file to which results should be printed. If **options.outfile** $[0] = \' \setminus 0'$  then the **stdout** stream is used.

Input: these options contain the names associated with the MPSX form of the problem. These names must be specified as follows:

prob\_name must contain the name of the problem to be read or be blank. The problem name is specified in the NAME indicator line (see Section 3) and if prob\_name is not blank, then nag\_opt\_sparse\_mps\_read will search the MPSX file for the specified problem. If prob\_name is blank, then the first problem encountered will be need.

**obj\_name** must contain the name of the objective row or be blank (in which case the first objective free row is used).

**rhs\_name** must contain the name of the RHS set to be used or be blank (in which case the first RHS set is used).

range\_name must contain the name of the RANGES set to be used or be blank (in which case the first RANGES set, if any, is used).

bnd\_name must contain the name of the BOUNDS set to be used or be blank (in which case the first BOUNDS set, if any, is used).

Constraints: the names must be valid MPSX names, i.e., they must consist only of the 'alphanumeric' characters as specified in Section 3 and must not contain leading blank characters.

Output: the members contain the appropriate names as read from the MPSX file. Any names specified on input which are not found in the MPSX file are unchanged on exit but will give rise to an error exit from nag\_opt\_sparse\_mps\_read (see Section 8).

If the MPSX file is successfully read, the **options** structure can be passed on to nag\_opt\_sparse\_convex\_qp (e04nkc), which will solve the problem specified by the file and which can make use of these structure members in its solution output.

 $col\_lo\_default - double$  Default = 0.0

Input: the default lower bound to be used for the variables in the problem when none is specified in the BOUNDS section of the MPSX data file.

### $col\_up\_default - double$

 $Default = 10^{20}$ 

Input: the default upper bound to be used for the variables in the problem when none is specified in the BOUNDS section of the MPSX data file.

Constraint:  $options.col\_up\_default \ge options.col\_lo\_default$ .

ncol\_approx - Integer nrow\_approx - Integer Default = 500

Default = 500

Input: an estimate of the number of columns and rows in the problem. nag\_opt\_sparse\_mps\_read is designed so that the problem size does not have to be known in advance, and allocates memory according to the data contained in the MPSX file. However, for very large problems, an advance estimate of the problem size might allow slightly more efficient memory usage to be achieved. See also the description of optional parameter **est\_density**.

Constraints:

 $\begin{aligned} & \textbf{options.ncol\_approx} > 0, \\ & \textbf{options.nrow\_approx} > 0. \end{aligned}$ 

est\_density - double

Default = 0.05

Input: an estimate of the density of the nonzeros in the sparse matrix A, i.e., an estimate of  $\operatorname{nnz} / (\mathbf{n} \times \mathbf{m})$ . As with the optional parameters  $\operatorname{ncol\_approx}$  and  $\operatorname{nrow\_approx}$ , if this is known to be significantly larger or smaller than the default, then the user should specify an appropriate value to aid  $\operatorname{nag\_opt\_sparse\_mps\_read}$  in its memory management.

Constraint: **options.est\_density** > 0.0.

crnames - char \*\*

Default memory  $\mathbf{n}+\mathbf{m}$  array of char \*

Output: the MPSX names of all the variables and constraints in the problem in the following order. **crnames**[j-1] contains the name of the jth column, for  $j=1,2,\ldots,\mathbf{n}$ . **crnames** $[\mathbf{n}+i-1]$  contains the name of the ith row, for  $i=1,2,\ldots,\mathbf{m}$ . Each name is 8 characters long, and includes any trailing blank characters which appear in the appropriate name field of the MPSX file.

Sufficient memory to hold the names is allocated internally by nag\_opt\_sparse\_mps\_read. The memory freeing function nag\_opt\_free (e04xzc) should be used to free this memory. Users should **not** use the standard C function free() for this purpose.

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If, on return from nag\_opt\_sparse\_mps\_read, nag\_opt\_sparse\_convex\_qp (e04nkc) is called with **options** as an argument, and the memory pointed to by **crnames** has not been freed, nag\_opt\_sparse\_convex\_qp (e04nkc) will use the row and column names stored in **crnames** in its solution output.

## 8. Error Indications and Warnings

#### NE\_NULL\_ARGUMENT

Argument **n** is a null pointer. It should contain the address of a variable of type Integer. Argument **m** is a null pointer. It should contain the address of a variable of type Integer. Argument **mnz** is a null pointer. It should contain the address of a variable of type Integer. Argument **iobj** is a null pointer. It should contain the address of a variable of type Integer. Argument **bl** is a null pointer. It should contain the address of a variable of type double \*. Argument **bu** is a null pointer. It should contain the address of a variable of type double \*. Argument **a** is a null pointer. It should contain the address of a variable of type double \*. Argument **ha** is a null pointer. It should contain the address of a variable of type Integer \*. Argument **ka** is a null pointer. It should contain the address of a variable of type Integer \*. Argument **xs** is a null pointer. It should contain the address of a variable of type double \*.

#### NE\_OPT\_NOT\_INIT

Options structure not initialized.

#### NE\_BAD\_PARAM

On entry, parameter options.prob\_name had an illegal value.

On entry, parameter **options.obj\_name** had an illegal value.

On entry, parameter options.rhs\_name had an illegal value.

On entry, parameter options.range\_name had an illegal value.

On entry, parameter **options.bnd\_name** had an illegal value.

On entry, parameter options.output\_level had an illegal value.

#### NE\_2\_REAL\_EE\_OPT\_ARG\_CONS

On entry, options.col\_lo\_default =  $\langle value \rangle$  while options.col\_up\_default =  $\langle value \rangle$ . Constraint: options.col\_lo\_default  $\leq$  options.col\_up\_default.

## NE\_INT\_OPT\_ARG\_LT

On entry, **options.nrow\_approx** =  $\langle value \rangle$ . Constraint: **nrow\_approx**  $\geq 1$  On entry, **options.ncol\_approx** =  $\langle value \rangle$ . Constraint: **ncol\_approx**  $\geq 1$ 

## NE\_INVALID\_REAL\_RANGE\_F

Value  $\langle value \rangle$  given to **options.est\_density** is not valid. Correct range is **est\_density** > 0.0.

### NE\_NAMES\_NOT\_NAG\_MEM

**options.crnames** is not null but does not point to memory allocated by an earlier call to this function. This function does not accept user-allocated memory assigned to **crnames**.

## NE\_MPS\_PROB\_NOT\_FOUND

The specified problem has not been found in the MPSX file.

#### NE\_MPS\_ILLEGAL\_DATA\_LINE

An illegal data line has been read from the MPSX file. This is neither a comment nor a legal data line.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

## NE\_MPS\_ILLEGAL\_NAME

An illegal row or column name has been detected. Names must contain only alphanumeric characters with no leading blanks.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

## NE\_MPS\_ILLEGAL\_NUMBER

Number expected but value could not be read. Check numerical fields.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

### NE\_MPS\_ILLEGAL\_SETNAME

An illegal name has been detected in field 2 of the RHS, RANGES or BOUNDS section. Names must contain only alphanumeric characters with no leading blanks.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

#### NE\_MPS\_INVALID\_BND\_TYPE

An invalid bound type appears in the BOUNDS section. Expect: LO, UP, FX, FR, MI, PL, BV or UI.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

#### NE\_MPS\_INVALID\_BND\_VAL

Invalid numeric field in bound data. Value expected for types: LO, UP, FX, UI. Blank field expected for types: FR, MI, PL, BV.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

#### NE\_MPS\_INVALID\_INDICATOR

Unknown, unexpected or invalid indicator line read. Expect: NAME, ROWS, COLUMNS, RHS, RANGES, BOUNDS or ENDATA, starting in column 1 of file, and in that order. RANGES and/or BOUNDS may be omitted.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

### NE\_MPS\_INVALID\_INTORG\_INTEND

An INTORG or INTEND marker is not correctly specified or is unexpected (e.g., INTEND has no matching INTORG).

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

#### NE\_MPS\_INVALID\_ROW\_TYPE

An invalid row type appears in the ROWS section. Expect: N, G, L or E.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

## NE\_MPS\_NO\_COLS

There were no columns specified in the COLUMNS section.

Last MPSX line read ( $\langle value \rangle$ ):  $\langle string \rangle$ .

#### NE\_MPS\_NO\_NEWLINE

New line expected but not found.

Last MPSX line read ( $\langle value \rangle$ ):  $\langle string \rangle$ .

## NE\_MPS\_NO\_OBJ

The objective row was not found. There must be at least one row of type N in the ROWS section and, if an objective name was specified, there must be a type N row with this name. Last MPSX line read ( $\langle value \rangle$ ):  $\langle string \rangle$ .

## NE\_MPS\_NO\_ROWS

There were no rows specified in the ROWS section.

Last MPSX line read ( $\langle value \rangle$ ):  $\langle string \rangle$ .

#### NE\_MPS\_REPEAT\_ROW

A row has been specified more than once.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

#### NE\_MPS\_RHS\_RANGE\_BND\_NOT\_FOUND

The name of the RHS, RANGES or BOUNDS set to be used was not found in the file.

#### NE\_MPS\_ENDATA\_NOT\_FOUND

The file does not contain an ENDATA indicator.

#### NE\_MPS\_SPLIT\_COL

Column data is not contiguous. All entries for a given column must appear together in the COLUMNS section.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

#### NE\_MPS\_UNKNOWN\_COLNAME

An unknown column name appears in the BOUNDS section. All the column names must be specified in the COLUMNS section.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

## NE\_MPS\_UNKNOWN\_ROWNAME

An unknown row name appears in the  $\langle string \rangle$  section. All the row names must be specified in the ROWS section.

Error at MPSX line  $\langle value \rangle$ :  $\langle string \rangle$ .

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#### NE\_ALLOC\_FAIL

Memory allocation failed.

#### NE\_NOT\_APPEND\_FILE

Cannot open file  $\langle string \rangle$  for appending.

#### NE\_WRITE\_ERROR

Error occurred when writing to file  $\langle string \rangle$ .

#### NE\_NOT\_CLOSE\_FILE

Cannot close file  $\langle string \rangle$ .

#### NE\_NOT\_READ\_FILE

Cannot open file  $\langle string \rangle$  for reading.

#### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

### 9. Further Comments

None.

#### 10. References

(1971) Program Number 5734 XM4 MPSX – Mathematical programming system IBM Trade Corporation, New York.

### 11. See Also

```
nag_opt_sparse_mps_free (e04myc)
nag_opt_sparse_convex_qp (e04nkc)
nag_opt_init (e04xxc)
nag_opt_read (e04xyc)
nag_opt_free (e04xzc)
```

### 12. Example 2

This example solves the same problem as Example 1 but illustrates the use of the **options** structure. Although the problem is the same, it is defined by a slightly modified MPSX file. The same **qphess** function is used as in Example 1.

The options structure is initialized by a call to nag\_opt\_init (e04xxc) and two of the optional parameters are set: prob\_name is set to "..QP 2.." so that nag\_opt\_sparse\_mps\_read will attempt to read a problem of this name; and obj\_name is set to "..COST..". The MPSX file (see Section 12.2) contains an additional free row, named "FREE ROW". Since this is the first free row in the ROWS section of the MPSX file, by default it would be read as the objective row. However, since obj\_name is specified, nag\_opt\_sparse\_mps\_read takes the second free row ("..COST..") as the objective row.

nag\_opt\_sparse\_mps\_read is called to read the MPSX file, and this is followed by a call to nag\_opt\_sparse\_convex\_qp (e04nkc) to solve the problem. As the **options** structure is passed as an argument, the row and column names read from the file are stored in **options.crnames** and used in the solution output (see Section 12.3).

Finally, nag\_opt\_sparse\_mps\_free (e04myc) is called to free the problem arrays, and nag\_opt\_free (e04xzc) is called to free the memory in **options**.

#### 12.1. Program Text

```
static void ex2(void)
#else
static void ex2()
#endif
{
```

```
Integer iobj, m, n, ncolh, nnz;
       Integer ninf;
      Integer *ha, *ka;
      double *bl, *bu, *a, *xs;
      double obj, sinf;
      Nag_E04_Opt options;
      static NagError fail, fail2;
      Vprintf("\nExample 2: use of options structure.\n");
      fail.print = TRUE;
      /* Initialize the options structure and read MPSX data */
      e04xxc(&options);
      Vstrcpy(options.prob_name, "..QP 2..");
Vstrcpy(options.obj_name, "..COST..");
      e04mzc((char*)0, &n, &m, &nnz, &iobj, &a, &ha, &ka, &bl, &bu, &xs,
              &options, &fail);
      /* Column and row names are now available via options */
      if (fail.code == NE_NOERROR)
        {
          ncolh = 5;
          e04nkc(n, m, nnz, iobj, ncolh, qphess, a, ha, ka, bl, bu, xs,
                  &ninf, &sinf, &obj, &options, NAGCOMM_NULL, &fail);
        }
       /* Free memory returned by e04mzc */
      e04myc(&a, &ha, &ka, &bl, &bu, &xs);
      /* Free memory in options (including column & row names) */ fail2.print = TRUE;
      e04xzc(&options, "all", &fail2);
12.2. Program Data
        ..ROW1..
        ..ROW2..
     L
     L
         ..ROW3..
     N FREE ROW
     N
        ..COST..
        COLUMNS
                                                            1.0
                                                            -4.0
                                                            2.0
                                                            3.0
                                                            -1.0
                                                            4.0
                                                            -1.0
                                                            -2.0
                                                            -1.0
                                                            1.0
                                                            -1.0
                                                             1.0
                                                            -1.0
                                                            1.0
                                                            -0.1
                                                            1.0
                                                            -0.3
    RHS
                 ..ROW1.. 1.5
..ROW2.. 1.5
        RHS1
        RHS1
        RHS1
                  ..ROW3..
                                4.0
    RANGES
        RANGE1 ..ROW1..
                                3.5
                 ..ROW2..
        RANGE1
                                3.5
        RANGE1
                 ..ROW3..
```

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BOUN	NDS			
LO	BOUND	X1	-2.0	
LO	BOUND	X2	-2.0	
LO	BOUND	X3	-2.0	
LO	BOUND	X4	-2.0	
LO	BOUND	X5	-2.0	
LO	BOUND	X6	-2.0	
LO	BOUND	X7	-2.0	
LO	BOUND	X8	-2.0	
LO	BOUND	X9	-2.0	
UP	BOUND	X1	2.0	
UP	BOUND	X2	2.0	
UP	BOUND	X3	2.0	
UP	BOUND	X4	2.0	
UP	BOUND	X5	2.0	
UP	BOUND	X6	2.0	
UP	BOUND	X7	2.0	
UP	BOUND	X8	2.0	
UP	BOUND	X9	2.0	
ENDATA				
ъ	ъ.	1.		

### 12.3. Program Results

# Parameters to e04mzc

prob\_name......QP 2.. 

col\_lo\_default..... 0.00e+00 output\_level.....Nag\_MPS\_Summary outfile..... stdout

MPS file successfully read. Number of lines read: 57 Number of columns: Number of rows:

5 (including objective row)

machine precision..... 1.11e-16

nrow\_approx.....

MPS Names Selected:

Problem ..QP 2..
Objective ..COST.. RHS
RANGES RANGE1 BOUNDS RHS1 BOUND

lu\_sing\_tol..... 2.04e-11

 $\ensuremath{\mathsf{MPS}}$  data successfully assigned to problem data.

## Parameters to e04nkc

Problem typesparse QP Linear constraints 5	Number of variables 9 Hessian columns 5
prob_name         .QP 2.           obj_name         .COST.           range_name         .RANGE1           crnames         .supplied	rhs_name
minimize         TRUE           ftol         1.00e-06           fcheck         60           scale         Nag_ExtraScale           optim_tol         1.00e-06           crash         Nag_CrashTwice           partial_price         10           max_sb         6	start
inf_bound	inf_step

```
print_level......Nag_Soln_Iter
outfile..... stdout
Memory allocation:
state.....
                             Nag
                                    lambda.....
                                                                  Nag
           Step
                         Sinf/Objective
  Tt.n
                  Ninf
                                          Norm rg
                           0.000000e+00
        0.0e+00
                   0
                                          0.0e+00
Itn
         0 -- Factorize detected a singular Hessian.
              Rank = 5, Diag, min diag = 0.0e+00, 3.3e-13.
    0
        0.0e+00
                     0
                           0.000000e+00
                                          6.3e+00
Itn 0 -- Feasible QP solution.
                  0
    1
        7.5e-01
                          -4.375000e+00
                                          3.5e-01
        1.0e+00
    2
                     0
                          -4.400000e+00
                                          0.0e + 00
                                          1.6e+00
    3
        1.9e-01
                     0
                          -4.700000e+00
        1.0e+00
                         -5.100000e+00
    4
                     0
                                          2.2e-16
Itn
         5 -- Hessian numerically indefinite.
                                          -1.4e-14,
                                                      2.7e-13.
              Square of diag, min diag =
    5
        2.2e-01
                     0
                          -5.932500e+00
                                          3.7e+00
        4.7e-01
    6
                     0
                          -6.179688e+00
                                          1.1e+00
        1.0e+00
    7
                     0
                          -6.267162e+00
                                          2.2e-16
    8
        8.1e-03
                     0
                          -6.532489e+00
                                          1.4e+00
        6.3e-01
    9
                          -7.583236e+00
                     0
                                          1.3e-15
    10
        1.0e+00
                     0
                          -8.067718e+00
                                          8.9e-16
   11
        1.0e+00
                          -8.067778e+00
                     0
                                          2.2e-16
Variable State
                      Value
                              Lower Bound Upper Bound
                                                        Lagr Mult
                                                                     Residual
...X1...
           UI.
                2.00000e+00
                              -2.0000e+00
                                            2.0000e+00
                                                        -8.000e-01
                                                                     0.000e+00
              -2.33333e-01
                              -2.0000e+00
...X2...
          SBS
                                            2.0000e+00
                                                         0.000e+00
                                                                     1.767e+00
...X3...
          SBS
              -2.66667e-01
                              -2.0000e+00
                                            2.0000e+00
                                                         0.000e+00
                                                                    1.733e+00
...X4...
           BS
               -3.00000e-01
                              -2.0000e+00
                                            2.0000e+00
                                                        0.000e+00
                                                                    1.700e+00
...X5...
          SBS
               -1.00000e-01
                              -2.0000e+00
                                            2.0000e+00
                                                        -1.570e-16
                                                                    1.900e+00
...X6...
           UL
                2.00000e+00
                              -2.0000e+00
                                            2.0000e+00
                                                        -9.000e-01
                                                                    0.000e+00
                                                                    0.000e+00
...X7...
          UT.
                2.00000e+00
                              -2.0000e+00
                                            2.0000e+00
                                                        -9.000e-01
...X8...
          SBS
              -1.77778e+00
                              -2.0000e+00
                                            2.0000e+00
                                                        1.761e-17
                                                                     2.222e-01
...X9...
          BS
                              -2.0000e+00
               -4.55556e-01
                                            2.0000e+00
                                                        -5.551e-17
                                                                     1.544e+00
Constrnt State
                              Lower Bound
                                                                     Residual
                                           Upper Bound
                                                        Lagr Mult
                      Value
               1.50000e+00
                              -2.0000e+00
                                           1.5000e+00
                                                        -6.667e-02
                                                                     0.000e+00
..ROW1..
         UT.
                              -2.0000e+00
                                            1.5000e+00 -3.333e-02
..ROW2..
           UL
                1.50000e+00
                                                                    0.000e+00
                              -2.0000e+00
                                            4.0000e+00
..ROW3..
           BS
                3.93333e+00
                                                         0.000e+00
                                                                    -6.667e-02
FREE ROW
           BS
                0.00000e+00
                                     None
                                                  None
                                                         0.000e+00
                                                                    0.000e+00
..COST..
           BS -1.07856e+01
                                     None
                                                  None -1.000e+00 -1.079e+01
Exit after 11 iterations.
Optimal QP solution found.
Final QP objective value = -8.0677778e+00
```

3.e04mzc. 18 [NP3275/5/pdf]