

# *Investigation of $\pi^+\pi^-$ and $\pi K$ - atoms*

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on behalf of DIRAC collaboration

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Constants

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# Contents

- 1 Introduction
  - General information on DIRAC
  - DIRAC setup
- 2 ChPT predictions
- 3  $A_{\pi^+\pi^-}$  atom
  - Production
  - Detection
  - Results
- 4  $\pi K$  atom
  - Observation
- 5 Long-lived atom
  - Data taking
- 6 Conclusion

# DIRAC collaboration



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KEK



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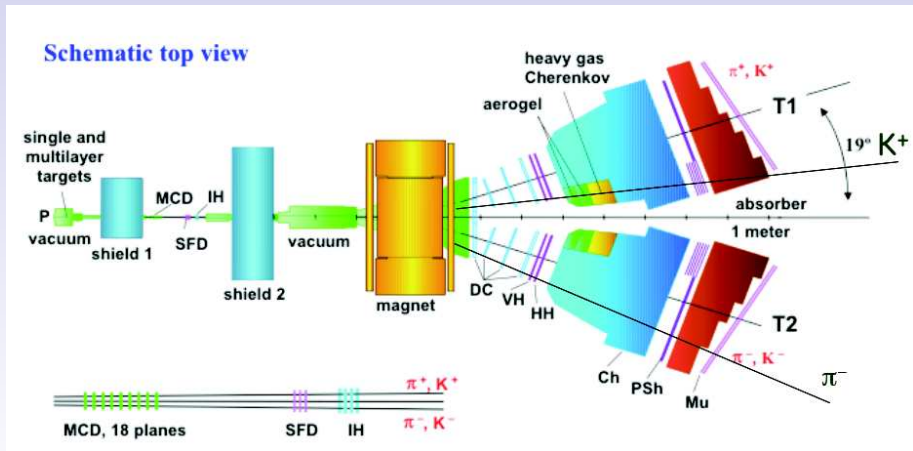
Kyoto Sangyou University

# Experiment DIRAC

**DIRAC** = **D**imeson **R**elativistic **A**tom **C**omplex

- using the proton beam (24 GeV/c) from PS at CERN
- detector : a double-arm magnetic spectrometer
- over 90 physicists from 24 institutes and universities
- data collection from 2001 (since that time several upgrades)
- **the main goals:**
  - 1 measurement of the lifetime of  $\pi^+\pi^-$  atom in the order of 3 fs with an accuracy of 10%
  - 2 after upgrade in 2006  $\rightarrow$  first observation of  $K\pi$  atoms, their lifetime and scattering length measurement
  - 3 long-lived atom observation

# DIRAC experimental setup



## ChPT predicts s-wave scattering lengths

$$\pi\pi: \quad a_0 = 0.220 \pm 0.005 \quad a_2 = -0.0444 \pm 0.0010$$

$$a_0 - a_2 = 0.265 \pm 0.004^1$$

*G. Colangelo et al., Nucl. Phys. B 603 (2001) 125*

$$\Rightarrow \tau = (2.9 \pm 0.1) \text{ fs}$$

$$(\Gamma = \frac{1}{\tau} \sim k|a_0 - a_2|^2)$$

$\pi K$ :

1-loop approx.

$$a_{1/2} = 0.19 \pm 0.02$$

$$a_{3/2} = -0.05 \pm 0.02$$

*V. Bernard, N. Kaiser, U. Meissner 1991*

$$a_{1/2} - a_{3/2} = 0.238 \pm 0.002$$

*B. Kubis, U.G. Meissner 2002*

2-loop approx.

$$a_{1/2} - a_{3/2} = 0.267$$

*J. Bijnens, P.P. Dhonte, P. Talavera 2004*

(Roy-Steiner equations)

$$a_{1/2} - a_{3/2} = 0.269 \pm 0.015$$

*P. Büttiker et al. 2004*

$$\Rightarrow \tau = (3.7 \pm 0.4) \text{ fs}$$

<sup>1</sup> the indices 0 and 2 refer to the isospin of the  $\pi\pi$ -system (1/2 and 3/2 refer to the isospin of the  $\pi K$ -system)

# Production of pionium

$\pi^+\pi^-$  atom - Coulomb bound state of two pions produced in one proton-nucleus interaction ( $N_A$ ).

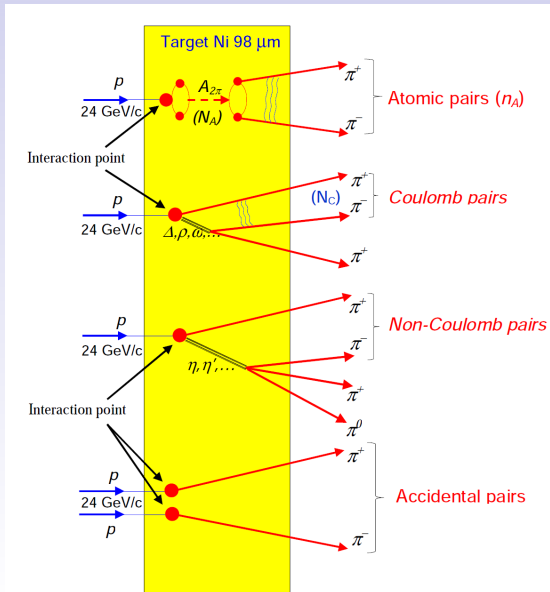
Atomic pairs - ionised  $\pi^+\pi^-$  atoms ( $n_A$ ).

## Background processes:

Coulomb pairs - produced in one proton-nucleus collision from fragmentation or short-lived resonances ( $\rho, \omega, \Delta$ ) and exhibit Coulomb interaction in the final state ( $N_C$ ).

Non-Coulomb pairs - produced in one proton-nucleus collision. At least one pion originates from a long-lived source ( $\eta, \eta', \dots$ ). No Coulomb interaction in the final state ( $N_{NC}$ ).

Accidental pairs - produced in two independent proton-nucleus collisions. No Coulomb interaction in the final state ( $N_{AC}$ ).



# Method of measurement

$\tau(A_{2\pi})$  is too small to be measured directly.

When pionium ( $A_{2\pi}$ ) moves through the target, following processes can occur:

## 1 Annihilation ... (strong interaction)

- $A_{2\pi} \rightarrow \pi^0 + \pi^0$  (decay ratio 99.6%,  $\tau \approx 3$  fs,  $A_{2\pi} \rightarrow \gamma\gamma$  contributes 0.36%)

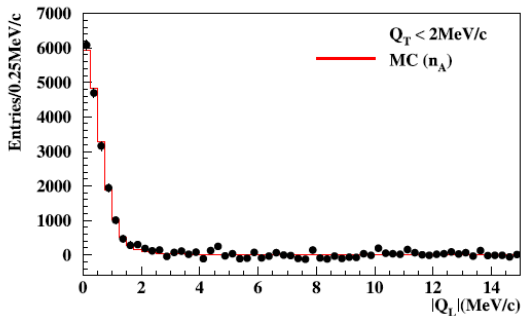
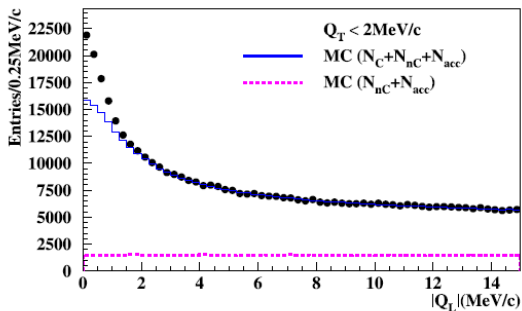
## 2 Excitation/Deexcitation ... (electromagnetic interaction)

- transition between atomic levels

## 3 Break-up (ionisation) ... (electromagnetic interaction)

- $A_{2\pi} \rightarrow \pi^+ + \pi^-$ ; characteristic "atomic pairs" ( $n_A$ )
- $Q_{CMS} < 3\text{MeV}/c$
- in LAB  $E_+ \approx E_-$ , small opening angle  $\Theta < 3\text{mrad}$

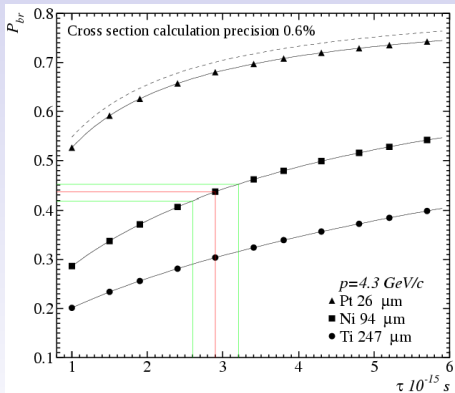




### Caption:

$|Q_L|$  fit projections of the  $\pi^+\pi^-$  spectrum from data (dots) and simulation (MC lines). The top plot shows the experimental spectrum compared with the simulated background components (no pionium signal), with (solid line) and without (dotted line) Coulomb pairs ( $N_{CC}$ ). The bottom plot shows the experimental  $|Q_L|$  spectrum after background subtraction and the simulated pionium spectrum.

# Break-up probability



an example of lifetime ( $2.9 \pm 0.3$ ) fs

## Calculation of $P_{br}$

$$P_{br} = \frac{n_A}{N_A} = \frac{n_A}{k N_{CC}}$$

- $n_A$  ... number of ionized  $A_{2\pi}$  atoms;  
 $N_A$  ... number of produced  $A_{2\pi}$  atoms
- there exists a precise relation between  $N_A$  and the total number  $N_{CC}$  of Coulomb pairs with small  $Q$  :  
 $N_A = k N_{CC}$   $k \approx 0.6 \dots Q \leq 2 \text{ MeV}/c$
- $P_{br}$  function of target material and thickness, atom lifetime  $\tau$  and  $A_{2\pi}$  momentum
- given lifetime  $\Rightarrow$  optimal target material

## Published results on ππ atom: lifetime &amp; scattering length

- the analysis of 2001-2003 data leads to the A<sub>2π</sub> lifetime  $\tau = (3.15 \pm 0.28)$  fs
- the derived scattering length difference is  $|a_0 - a_2| = (0.2533 \pm 0.011)m_\pi^{-1}$

DIRAC data	$\tau$ 1s (10–15s)					$ a_0 - a_2 $					Reference
	value	stat	syst	theo*	tot	value	stat	syst	theo*	tot	
2001	2.91	+0.45 -0.38	+0.19 -0.49	[+0.49 -0.62]		0.264	+0.017 -0.020	+0.022 -0.009	[+0.033 -0.020]		PL B 619 (2005) 50
2001-03	3.15	+0.20 -0.19	+0.20 -0.18	[+0.28 -0.26]		0.2533	+0.0078 -0.0080	+0.0072 -0.0077	[+0.0106 -0.0111]		PL B 704 (2011) 24

\* theoretical uncertainty included in systematic error

NA48	K-decay	$a_0 - a_2$					Reference
		value	stat	syst	theo	tot	
2009	K3π	0.2571 ± 0.0048 ± 0.0029			0.0088		EPJ C64 (2009) 589
2010	Ke4 & K3π	0.2639 ± 0.0020 ± 0.0015					EPJ C70 (2010) 635

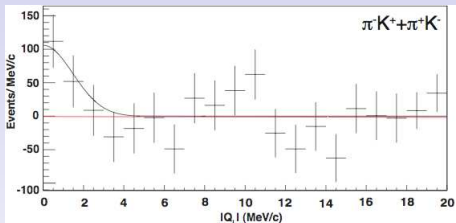
# $\pi K$ atom - motivation

- the study of electromagnetically bound hadronic pairs allows us to probe the low energy QCD
- the low energy interaction between the pion and the kaon (which contains the strange quark) is a proper tool to study the 3-flavour (u,d,s) structure of hadronic interaction or quark condensate in Chiral Perturbation Theory
- a measurement of the  $\pi K$ -atom lifetime is an important tool to determine the difference  $|a_{1/2} - a_{3/2}|$  of the s-wave  $\pi K$ -scattering lengths <sup>2</sup>

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<sup>2</sup>the indices 1/2 and 3/2 refer to the isospin of the  $\pi K$ -system

# $\pi K$ atom signal



Residuals between data and the fitted background for  $\pi^+ K^-$  and  $\pi^- K^+$ . A Gaussian fit has been applied (solid line) to illustrate the distribution of atomic-pairs.

**$277 \pm 52$   $\pi K$  atoms  
were observed**  
with a significance of  $5.3\sigma$

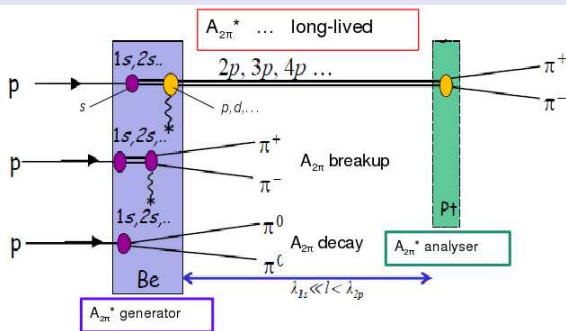
## numbers of $\pi K$ atoms

$\pi^- K^+$	$157 \pm 43$
$\pi^+ K^-$	$120 \pm 29$

The ultimate goal of the DIRAC experiment is to measure the lifetime of  $K\pi$  atoms with a precision of **20%** (or better).

# Long-lived atom - observation

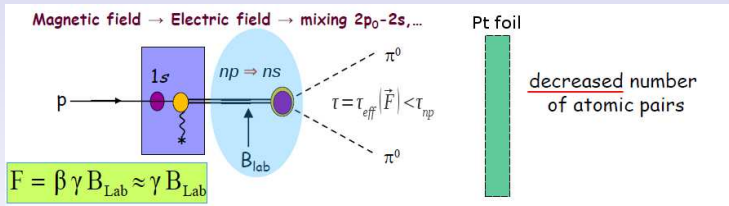
- $\sim 6\%$  of the atoms  $A_{2\pi}$ , generated in the target, exit the target in a long-lived state  $A_{2\pi}^*$  (mainly  $1s \rightarrow np$ )
- the main part of these atoms are in the  $2p$ -state
- the  $A_{2\pi}^*(np)$  decay into two  $\pi^0$  is forbidden<sup>3</sup> and  $A_{2\pi}^* \rightarrow \pi^0 + \gamma$  is also strongly suppressed
- the lifetime of the  $A_{2\pi}^*$  atom in the  $2p$  state ( $\tau_{2p} = 1.17 \times 10^{-11}\text{s}$ ) is determined by the  $2p \rightarrow 1s$  radiative transition with subsequent annihilation from  $1s$  state ( $\tau_{1s} \approx 3 \times 10^{-15}\text{s}$ )  
 $\Rightarrow$  the lifetime in  $np$ -states is about  $10^3$  times larger than for  $ns$ -states



<sup>3</sup>the conservation law of the angular momentum

# Long-lived atoms - “Lamb shift” measurement

- it is possible to measure **the 2s – 2p energy splitting** by exerting a **magnetic field** ( $\Rightarrow$  an electric field  $F$ ) on the atom  $\Rightarrow$  measurement of the decay probability dependence on the field (mixing of  $ns$  and  $np$ -states in the electric field)<sup>4</sup>



- electric field influences  $A_{2\pi}^*$  lifetime  $\tau_{eff} \Rightarrow$  “Lamb shift”  $\Delta E_{2s-2p}$   
 $\Rightarrow$  S-wave pion-pion scattering length combination  $2a_0 + a_2$

<sup>4</sup> a small admixture of the 2s-state in the 2p-state  $\rightarrow$  faster decay; for  $B_0=4$  T and  $\gamma = 20$  the decay rate increases more than a factor of two

# Conclusion

- the lifetime of  $A_{2\pi}$  atoms and the absolute value of difference of  $\pi\pi$  scattering lengths were measured

$$\tau = (3.15 \pm 0.28) \text{ fs}$$

$$|a_0 - a_2| = (0.2533 \pm 0.011) m_\pi^{-1}$$

- the number of  $\pi K$  atoms detected by DIRAC corresponds to more than  $5\sigma$  effect
- our goals for future:
  - a measurement of the  $\pi K$  atom lifetime
  - till the end of 2012 an observation of the  $\pi\pi$  long-lived atoms  $A_{2\pi}^*$



**Thank you for your attention!**

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**The Czech Technical University**

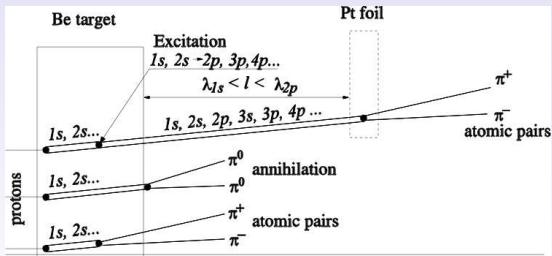
The Faculty of Nuclear Sciences and Physical Engineering  
The Department of Dosimetry and Application of Ionising Radiation  
Břehová 7, Prague 1  
the Czech Republic

Published results on  $\pi\pi$  atom: lifetime & scattering length - II.

- based on more than 21000 breaking  $A_{2\pi}$  atoms  
     $\Rightarrow$  statistical accuracy better than 10%
- to decrease systematic error, multiple scattering and an admixture of  $K^+K^-$  and  $p\bar{p}$  pairs are measured
- systematic error due to detector response is estimated

# Long-lived atoms - few numbers

- as the best target has been found 100  $\mu\text{m}$  thick Be target
- the corresponding decay length is 5.7 cm for  $2p$ -state, 19 cm for  $3p$ -state, 44 cm for  $4p$ -state, 84.5 cm for  $5p$ -state ( $\gamma=16.1$  in DIRAC)
- as the break-up foil has been chosen Pt foil with thickness of 2  $\mu\text{m}$ <sup>5</sup>
- the shortest distance between the Be target and the Pt foil can be around 10 cm to avoid interactions of the primary beam halo with the foil



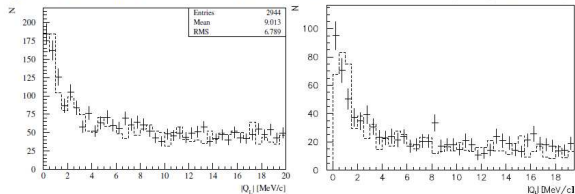
<sup>5</sup>the breakup probability of long-lived states is 0.94

# Production of $A_{2\pi}$ in the Be target

2010  
2011

$N_A = 736 \pm 75$   
 $N_A = 368 \pm 32$

Distribution over  $|Q_L|$  of  $\pi^+\pi^-$  pairs collected in 2010 (left) and in 2011 (right) with Beryllium target with the cut  $Q_T < 1$  MeV/c. Experimental data (points with error bars) have been fitted by a sum of the simulated distribution of "Coulomb" and "non-Coulomb" pairs (dashed line).



Produced atom numbers normalized on the proton flux:

$$N_{A_{2\pi}}/p = (5.1 \pm 0.5) \times 10^{-14} \text{ (2010)}$$

$$N_{A_{2\pi}}/p = (5.9 \pm 0.5) \times 10^{-14} \text{ (2011)}$$

The dependence of  $A_{2\pi}$  lifetime in  $2p$ -state  $\tau_{eff}$  from a strength of the electric field  $F$

$$\tau_{eff} = \frac{\tau_{2p}}{1+120|\xi|^2}$$

where

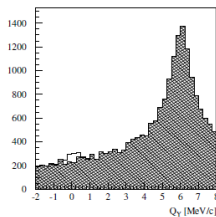
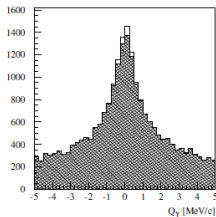
$$|\xi|^2 \approx \frac{F^2}{(E_{2p} - E_{2s})}$$

$$B_{Lab} = 4 \text{ Tesla} \left\{ \begin{array}{l} \gamma = 20, \quad |\xi| = 0.1 \Rightarrow \tau_{eff} = \frac{\tau_{2p}}{2.2} \\ \gamma = 40, \quad |\xi| = 0.2 \Rightarrow \tau_{eff} = \frac{\tau_{2p}}{6} \end{array} \right.$$

**SPS(450GeV):** yield of  $A_{2\pi}$  and  $A_{\pi K}$  will increase of a factor 20 per proton-nucleus interaction.

# Simulation of the permanent magnet influence

Simulated "atomic pairs" from long-lived atoms (light area) over  $Q_Y$  above the background of  $\pi^+\pi^-$  pairs produced in Beryllium target with cuts  $|Q_X| < 1$  MeV/c,  $|Q_L| < 1$  MeV/c (hatched area). In left side without the magnet and in right side with magnet used in 2011



Simulated distribution of  $\pi^+\pi^-$  pairs over  $Q_Y$  produced in Beryllium target with cuts  $|Q_X| < 1$  MeV/c,  $|Q_L| < 1$  MeV/c. The events without magnet (solid line) are distributed around 0 and events with the new magnet are shifted by 15 MeV/c (dashed line)

