

Bose-Einstein Correlations

The legacy of LEP and SLC

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On behalf of the LEP collaborations

Introduction

Identical bosons obey Bose-Einstein statistics

- Constructive interference between identical bosons in multi-hadronic final states
- Enhancement of number of identical bosons over number of non identical bosons close in phase space
- First observed in like-sign charged pion pairs in $p\bar{p}$ annihilations

BEC may influence the properties of multi-hadronic final states:

LEPI: $ee \rightarrow Z \rightarrow qq \rightarrow \text{hadrons}$

LEPII: $ee \rightarrow WW \rightarrow qq\bar{q}\bar{q} \rightarrow \text{hadrons}$

Bose Einstein Correlations (BEC)

- Studied as a function of Q :

$$Q^2 = -(\mathbf{p}_1 - \mathbf{p}_2)^2 \quad \mathbf{p}_{1,2} = 4 - \text{momentum}$$

- Using the two-particle correlation function

$$R(Q) = \frac{\mathbf{r}(Q)}{\mathbf{r}_0(Q)} \quad \mathbf{r}(\mathbf{p}_1, \mathbf{p}_2) = \frac{1}{N_{\text{ev}}} \frac{dn_{\text{pairs}}}{dQ}$$

$$R(Q) = 1$$

In the absence
of BEC

ρ : two particle density

$\rho_0 = \rho_{\text{no BE}}$ (reference sample)

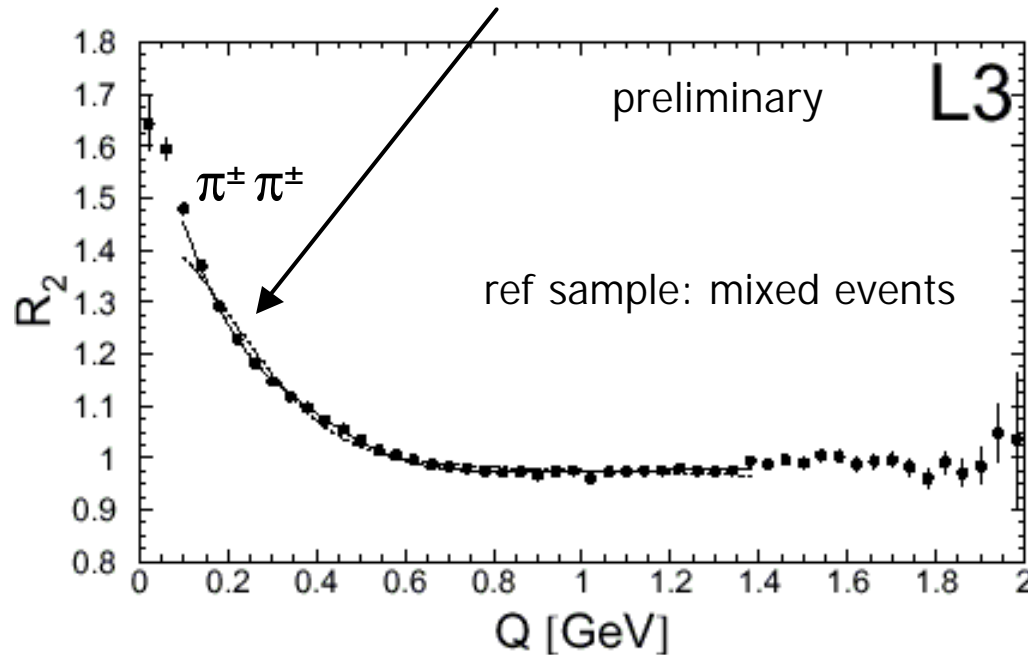
- ❖ Unlike sign charged particle pairs
 - ❖ 'mixed events'
 - ❖ MC without BEC
- } Double ratio: $R_{\text{data}}/R_{\text{MC no BE}}$

LEP I

$Z \rightarrow qq \rightarrow \text{hadrons}$

$\pi^\pm\pi^\pm$

Enhancement at low values of Q



Fit assuming a spherical source of BEC with gaussian density:

$$R(Q) \approx 1 + I \exp(-r^2 Q^2)$$

λ : strength of the correlation

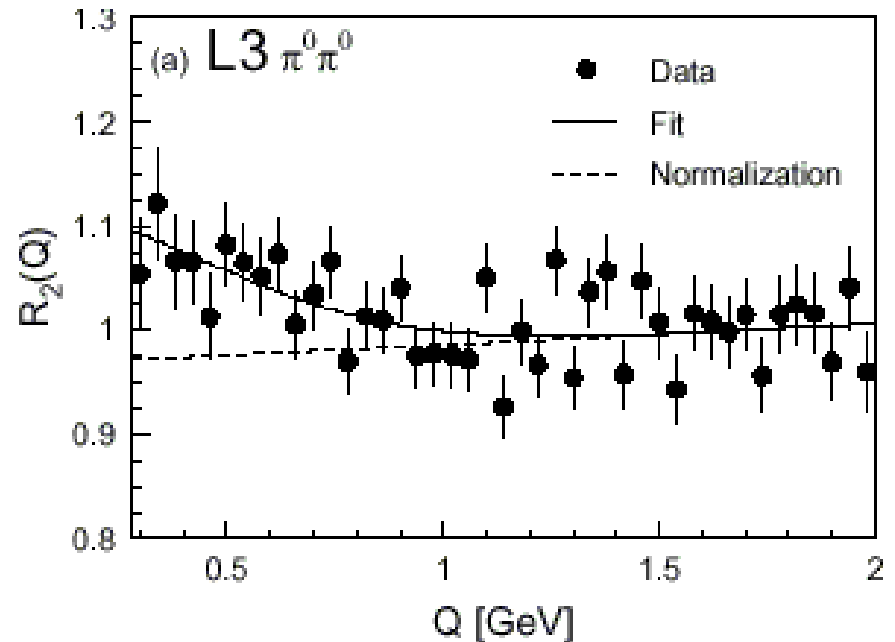
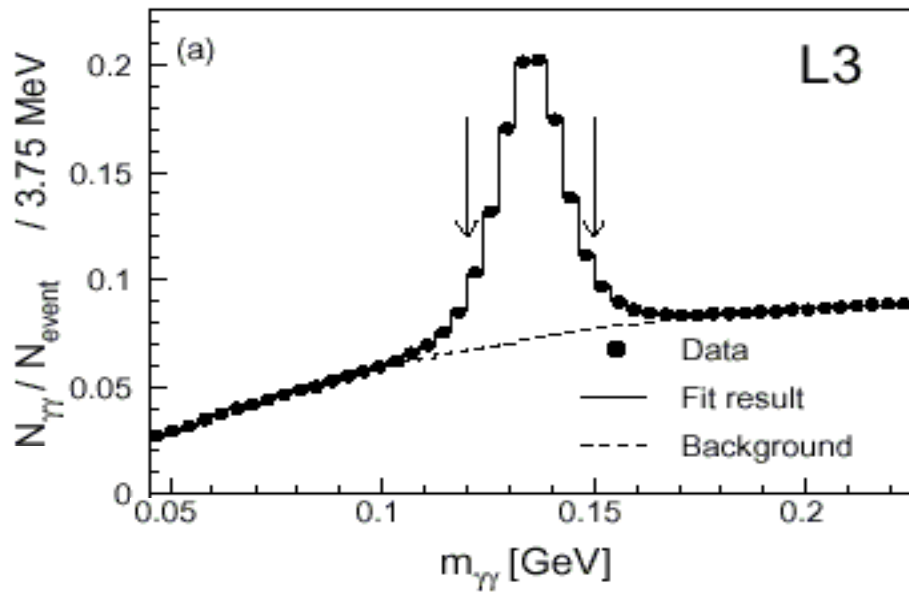
r : source size

λ significantly different from zero (also measured by A,D,O)

$r \sim 0.5-1.0$ fm

A,D,L,O { different reference samples
different fragmentation parameters (JETSET)

$\pi^0\pi^0$

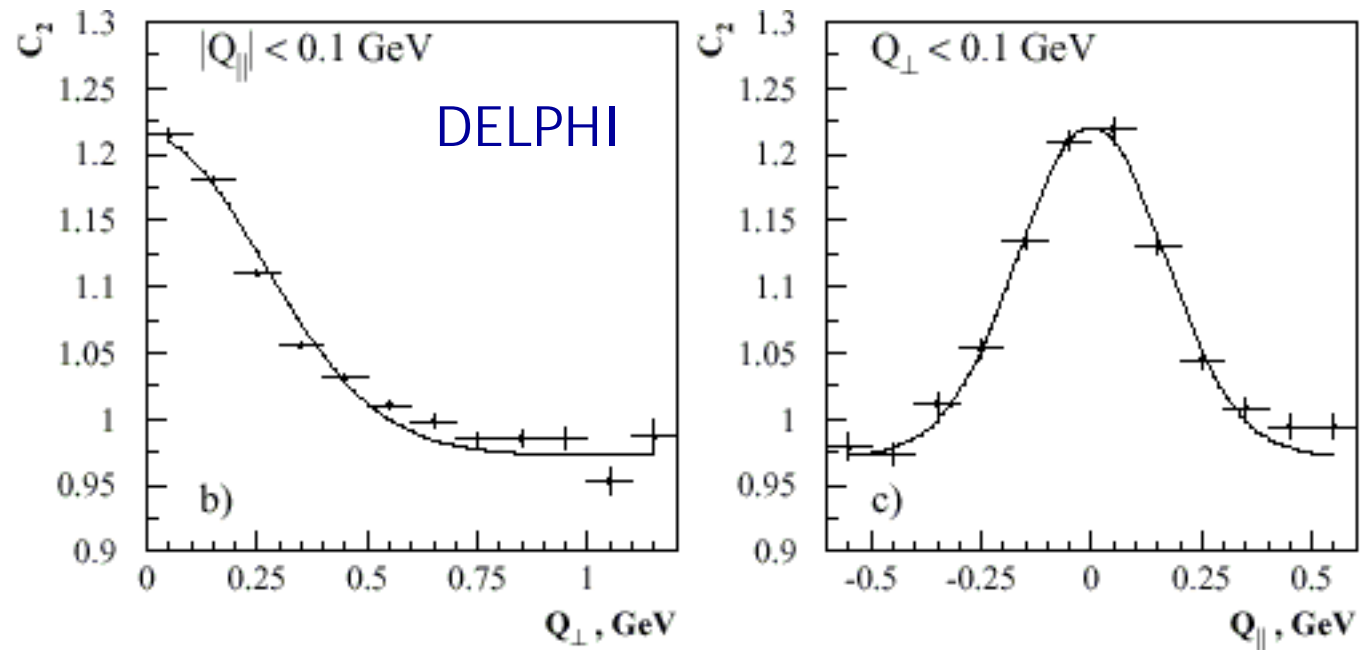
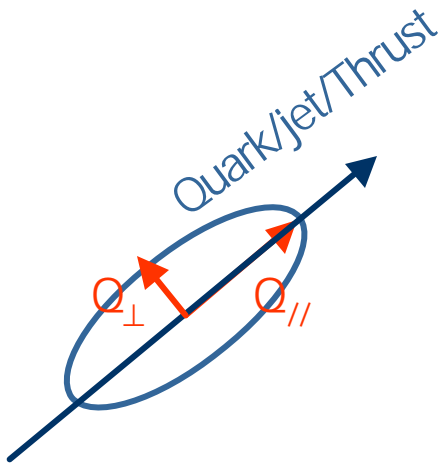


$$r_{\pm\pm} - r_{00} = 0.150 \pm 0.075(\text{st}) \pm 0.068(\text{sys}) \text{ [fm]}$$

same reference sample for $\pi^0\pi^0$ and $\pi^\pm\pi^\pm$

indication of smaller radius for the neutral pion source

2-Dim analysis of the source



	r_{\perp}/r_{\parallel}	Method
DELPHI	$0.62 \pm 0.02 \pm 0.05$	Mixed events
OPAL	$0.73 \pm 0.02 \pm 0.07$	Unlike-Charge
L3	$0.81 \pm 0.02^{+0.03}_{-0.19}$	Mixed events

- evidence for the elongation of the pion source
- implications for modeling of BEC in hadronic final states

Three particle correlations

- Studied as a function of Q_3 :

$$Q_3^2 = Q_{12}^2 + Q_{13}^2 + Q_{23}^2$$

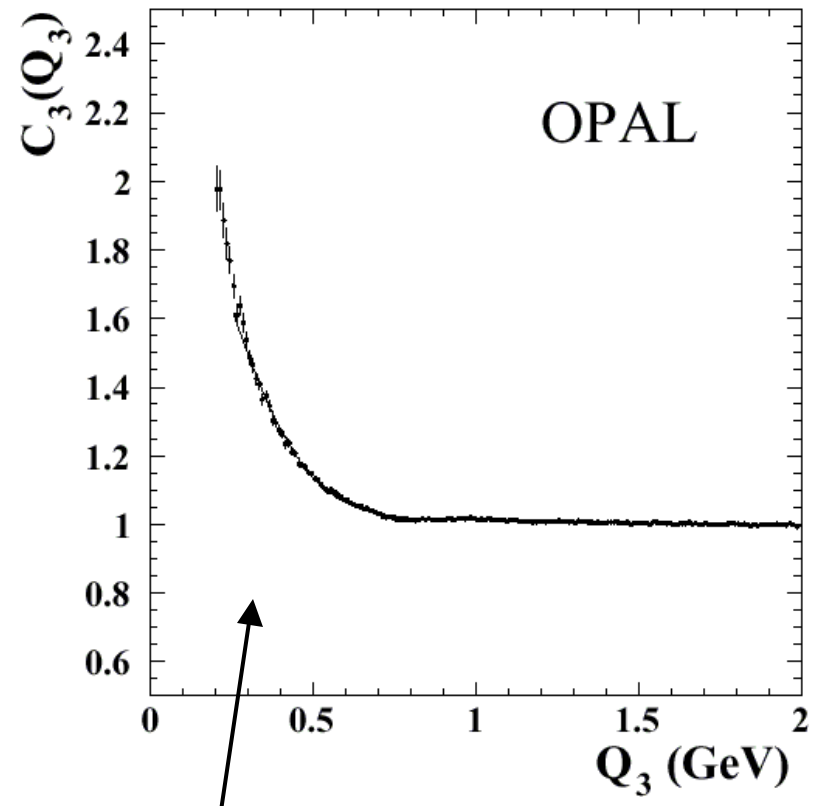
- Using the three particle correlation function:

$$R_3(Q) = \frac{\mathbf{r}_3(p_1, p_2, p_3)}{\mathbf{r}_0(p_1, p_2, p_3)}$$

- C_3 : genuine 3 boson correlation

$$C_3(Q_3) = R_3 - R_{1,2}$$

Two-boson correlation contribution



Enhancement at low values of Q_3
(also observed by D,L)

Conclusions from LEPI analyses

- Bose-Einstein Correlations are observed in hadronic Z decays
- Indication of smaller radius for $\pi^0\pi^0$ than $\pi^\pm \pi^\pm$
- Evidence for the elongation of the BEC source
- Three particle correlations also observed

Other analyses done at LEPI

- Dependence of source size on hadron mass
- BEC in $K^\pm K^\pm$ and $K_s^0 K_s^0$
- Multiplicity dependence of BEC

LEP II

$WW \rightarrow qq\bar{v}$

$WW \rightarrow qq\bar{q}\bar{q}$

BEC in $e^+e^- \rightarrow WW$

- BEC inside W in hadronic W decays (inter- W)
- BEC between two W 's in fully hadronic decays (intra- W)
 - Distance between the two W decay vertices: 0.1 fm
 - Hadronization scale: 0.5-1 fm

} Space-time overlap

If intra- W BEC exist:

momentum transfer between the two W 's can affect the W mass measurement in $qqqq$ channel

Systematic error on the W mass

$$\Delta M_W^{\text{BEC}} = 20 - 67 \text{ MeV}$$

} Summer 2001

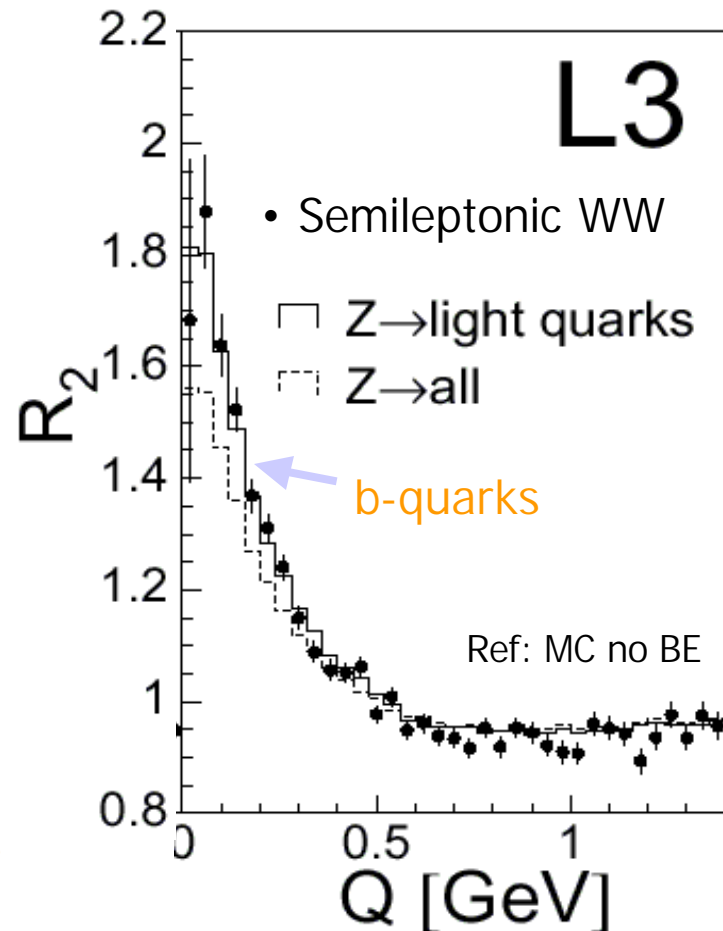
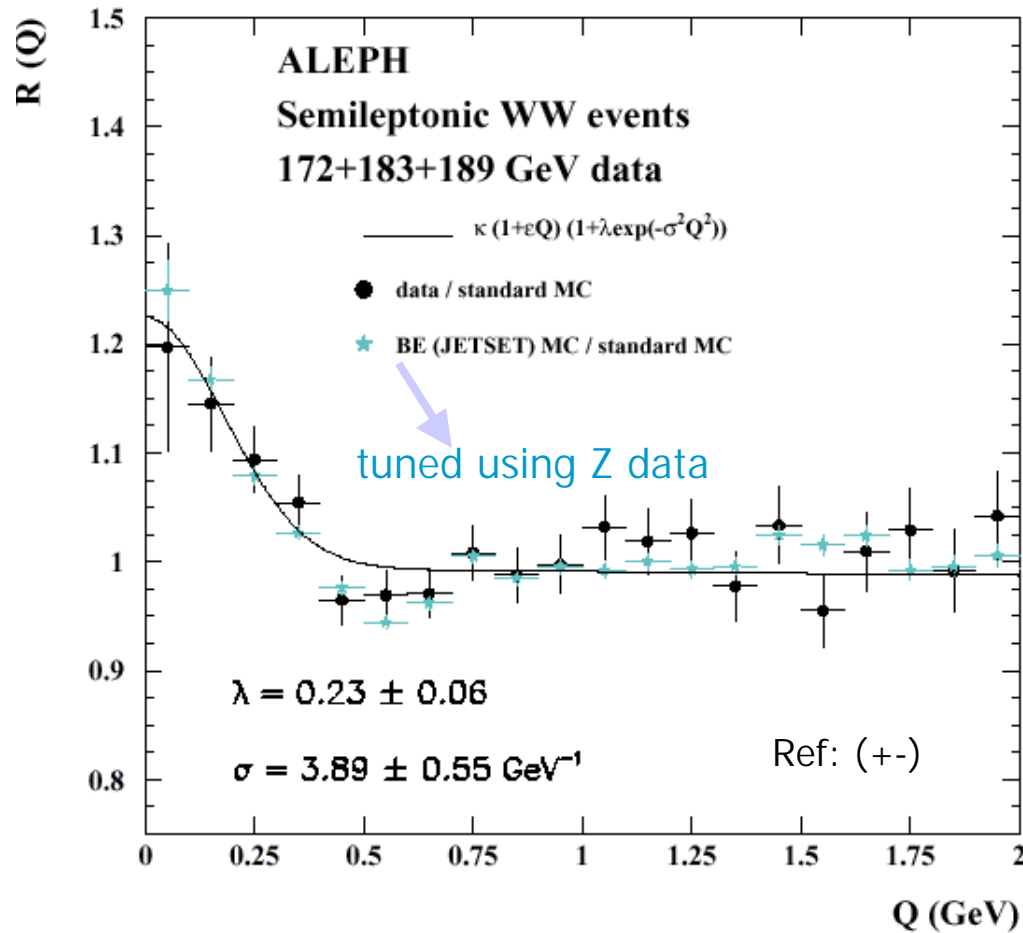
} A,D,L,O

BE Models

- Models of **Sjöstrand/Lönnblad** (LUBOEI)
 - 2 particle correlations introduced artificially by reshuffling momenta of final hadrons
 - E/P transfer between Ws to ensure global E/P conservation
 - Models are tuned using hadronic Z decays
- **Reweighting** models
 - conserve E/P and include QM calculations
 - But... very difficult to implementation (**negative and large weights**) – **not used for the time being.**

Intra W correlations

$WW \rightarrow qq\ell\nu$

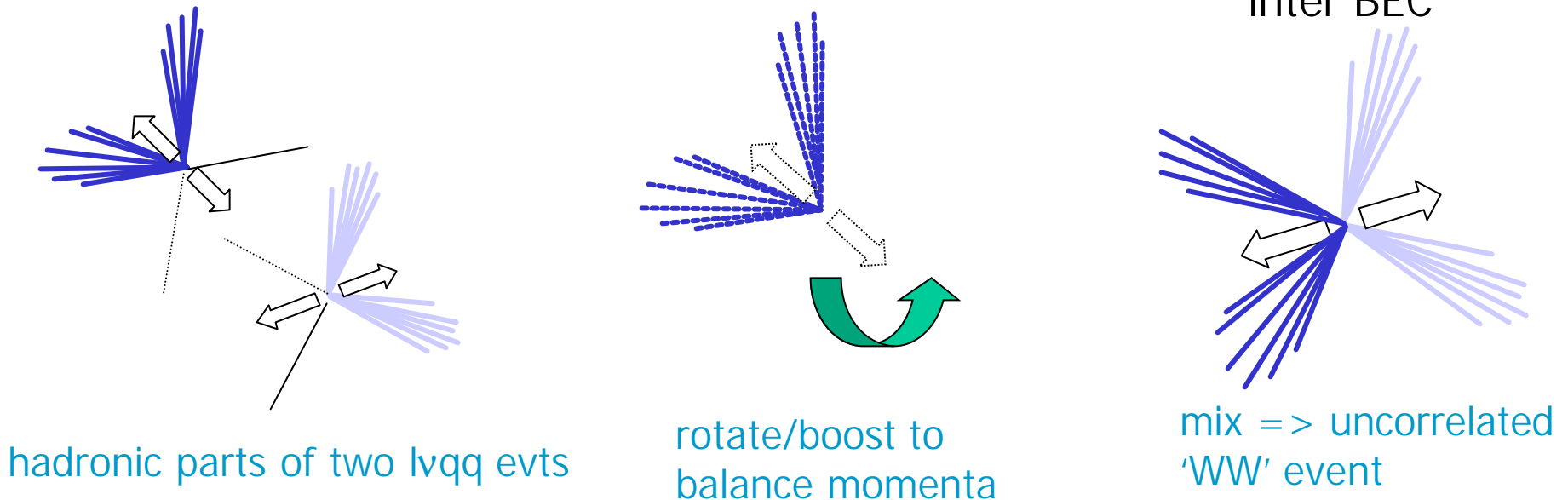


Evidence for BEC inside W's

Inter-W BEC

Analysis à la Chekanov, De Wolf, Kittel (Eur. Phys. J. C6 (1999) 403)

$$\Delta \mathbf{r} = \mathbf{r}^{\text{WW} \rightarrow 4\text{q}} - (2\mathbf{r}^{\text{W} \rightarrow 2\text{q}} + \mathbf{r}^{\text{WW}_{\text{mix}}}) \longrightarrow \Delta p = 0 \text{ in the absence of inter BEC}$$



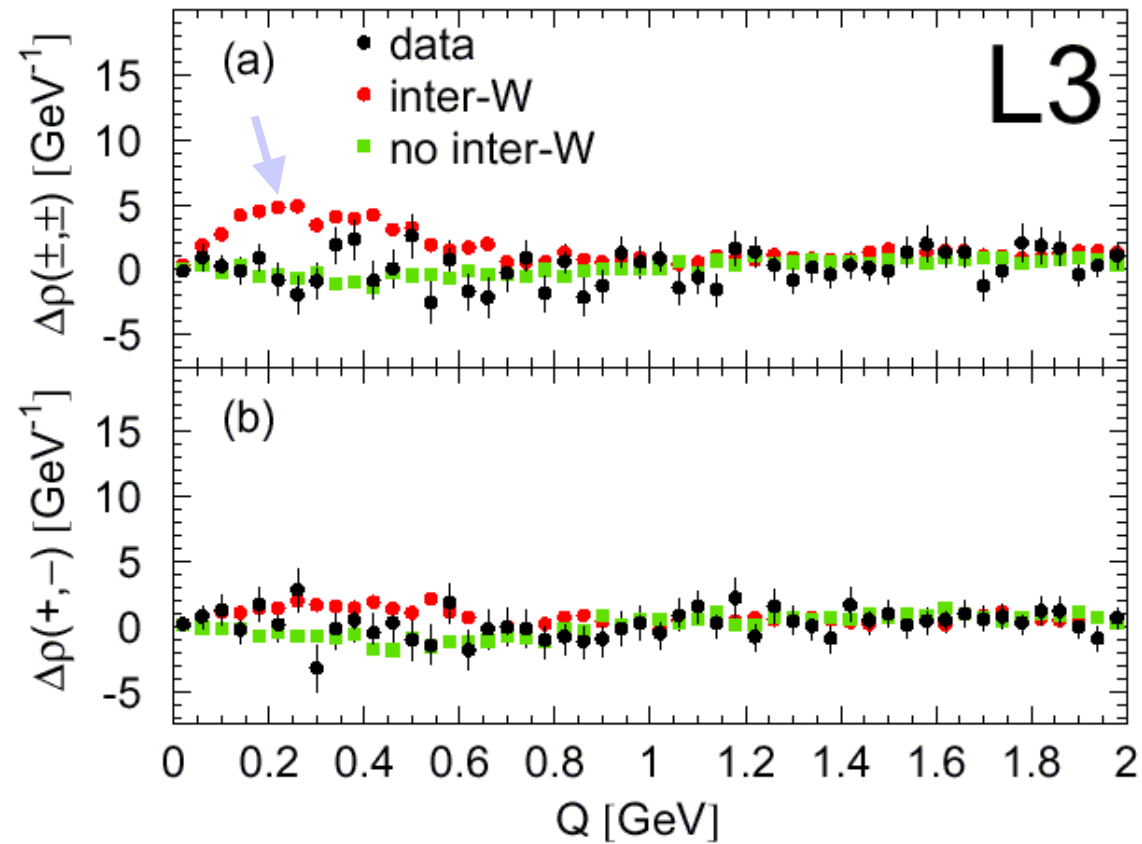
- Experimentally robust (data compared with data)
- Model independent (except for background subtraction)

ABSOLUTE MEASUREMENT OF INTER-W CORRELATIONS

Inter W BEC

Data
compatible with
NO inter W BEC

Small artificial
enhancement for
 $\Delta r(+,-)$
due to BE
simulation



Strength of the inter W BEC

$$D = \frac{\mathbf{r}^{WW \rightarrow 4q}}{2\mathbf{r}^{W \rightarrow 2q} + \mathbf{r}^{WW_{\text{mix}}}}$$

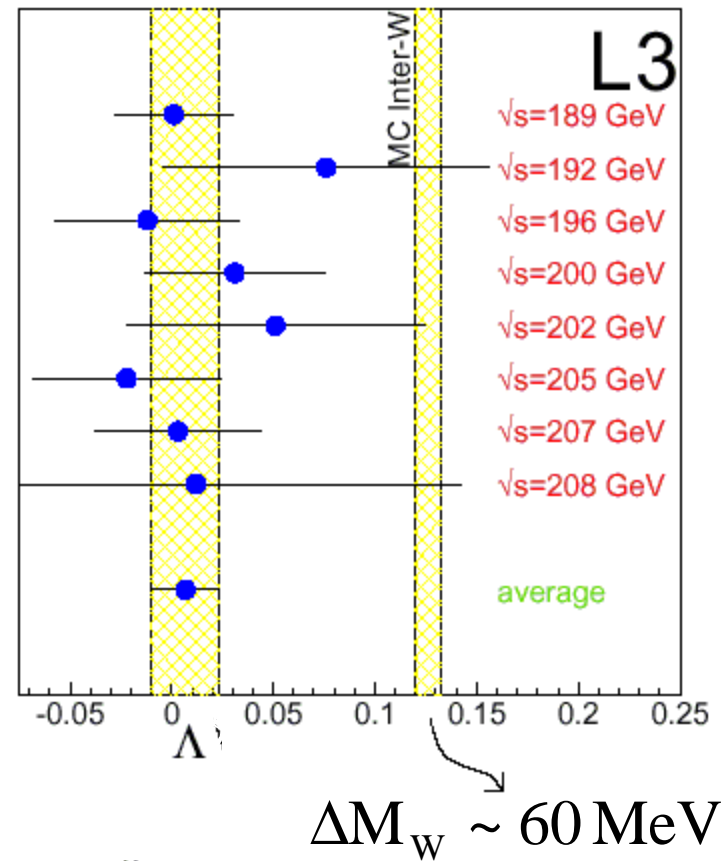
$$D' = \frac{D^{\text{data}}}{D^{\text{MC}}_{\text{no BE}}}$$

} $D'=D=1$ in the absence in inter-W BEC

Fit: $D'(Q) \approx 1 + \Lambda \exp(-k^2 Q^2)$

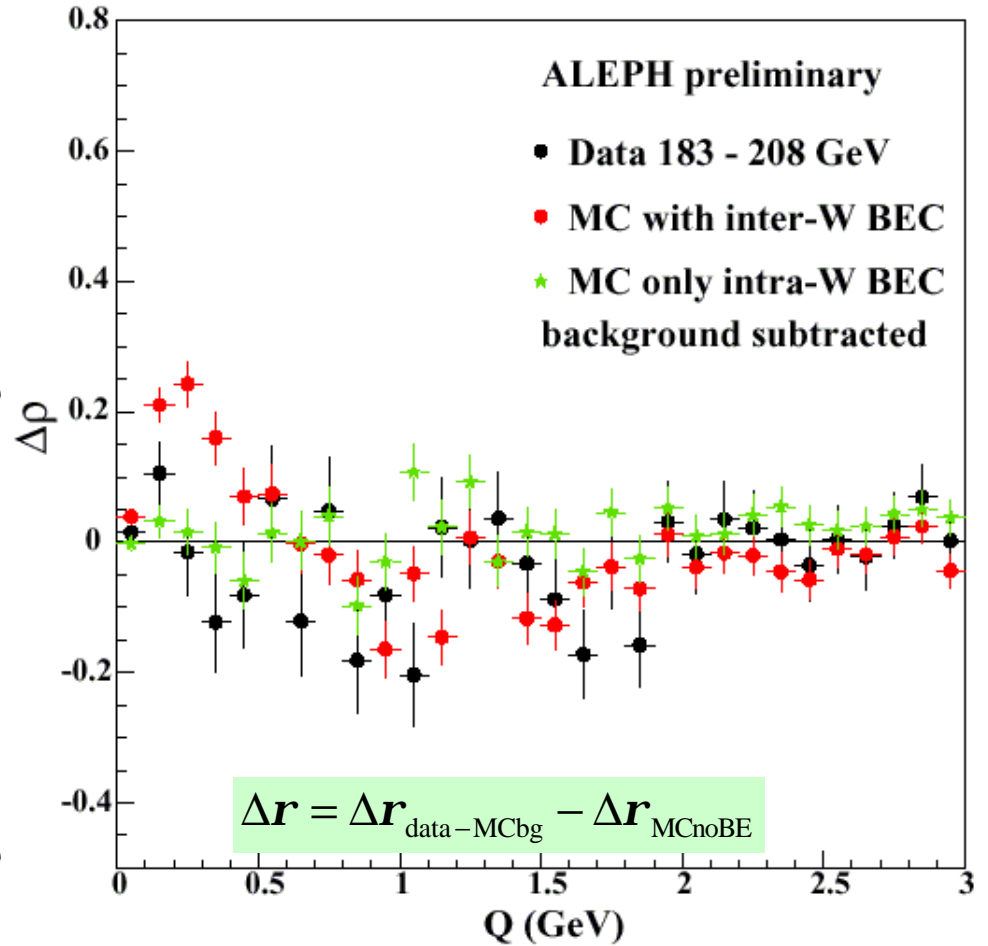
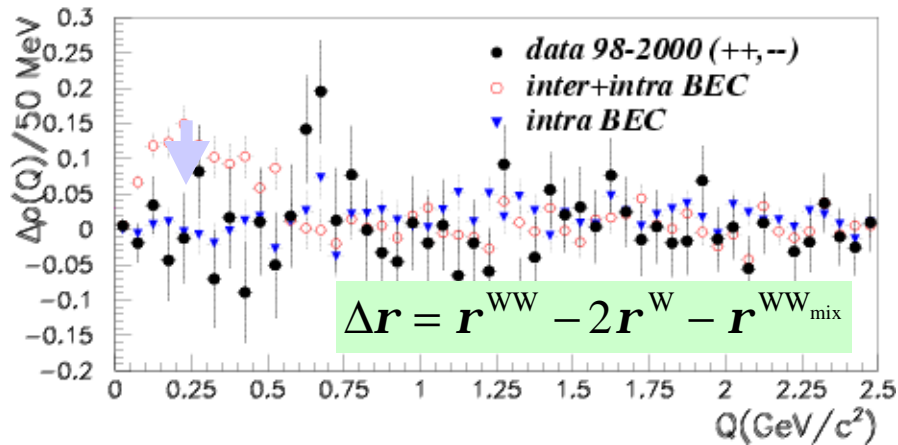
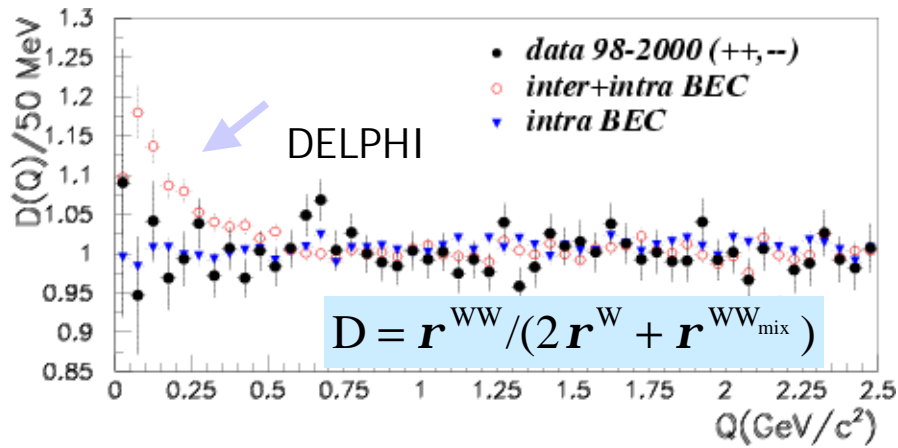
$\Lambda^{\text{data}} = 0.008 \pm 0.018(\text{st.}) \pm 0.016(\text{sy.})$

$\Lambda^{\text{MC}}(\text{interWW}) = 0.126 \pm 0.008(\text{st.})$



Inter WW BEC are disfavored

Inter W BEC



NO correlations between different Ws observed

OPAL analysis with mixing method in progress

Conclusions from LEP II analyses

- BEC exist inside W's
- Similar effect in Z and W decays
- No evidence for the existence of inter-W correlations
 - Not taken into account yet for ΔM_W^{BEC}