

# 1 Extra Material

## 1.1 $f_{A_b^0}/f_d$ data points

The measured values of  $f_{A_b^0}/f_d$  in bins of  $p_T$  and  $\eta$  are given in Tables 1 and 2, respectively.  $f_{A_b^0}/f_d$  is calculated as  $\mathcal{R} \times \mathcal{S}$ , where  $\mathcal{R}$  is the efficiency corrected yield ratio. The data points correspond to those shown in Fig. 3 in the paper. In the above mentioned tables, the uncertainties only include the *uncorrelated* statistical uncertainties on the measured yields and efficiencies. For convenience, the information from Tables 1 and 2 can be found in the plain text files *flfd\_datapoints\_pt.txt* and *flfd\_datapoints\_eta.txt*.

## 1.2 Correlated uncertainties

In addition to the *uncorrelated* uncertainties shown in Tables 1 and 2, there are two sources of *correlated* uncertainty that contribute to the total uncertainty on  $f_{A_b^0}/f_d$ .

$p_T$ bins [GeV/c]		$f_{A_b^0}/f_d$
boundaries	mean	
1.5 - 3.6	2.53	$0.571 \pm 0.015$
3.6 - 4.5	4.04	$0.543 \pm 0.014$
4.5 - 5.3	4.89	$0.496 \pm 0.012$
5.3 - 6.0	5.64	$0.510 \pm 0.012$
6.0 - 6.5	6.24	$0.469 \pm 0.012$
6.5 - 7.0	6.74	$0.424 \pm 0.011$
7.0 - 7.5	7.24	$0.398 \pm 0.010$
7.5 - 8.0	7.74	$0.484 \pm 0.012$
8.0 - 8.5	8.24	$0.432 \pm 0.011$
8.5 - 9.0	8.74	$0.406 \pm 0.011$
9.0 - 9.5	9.24	$0.388 \pm 0.010$
9.5 - 10.0	9.74	$0.390 \pm 0.011$
10.0 - 10.7	10.34	$0.342 \pm 0.008$
10.7 - 11.5	11.08	$0.344 \pm 0.008$
11.5 - 12.2	11.84	$0.350 \pm 0.010$
12.2 - 13.0	12.58	$0.371 \pm 0.011$
13.0 - 14.3	13.61	$0.278 \pm 0.007$
14.3 - 16.0	15.08	$0.277 \pm 0.008$
16.0 - 20.2	17.73	$0.251 \pm 0.006$
20.2 - 40.0	24.85	$0.214 \pm 0.007$

Table 1:  $f_{A_b^0}/f_d$  in bins of  $p_T$  of the  $b$  hadron. The uncertainties include the statistical uncertainty on the measured yields. The systematic uncertainty and the uncertainties originating from the scale factor  $\mathcal{S}$  are not included. The statistical uncertainty on the measured efficiency is treated as a systematic uncertainty.

$\eta$ bins		$f_{A_b^0}/f_d$
boundaries	mean	
2.00 - 2.60	2.32	$0.321 \pm 0.006$
2.60 - 2.75	2.68	$0.359 \pm 0.008$
2.75 - 2.90	2.82	$0.364 \pm 0.007$
2.90 - 3.05	2.97	$0.386 \pm 0.007$
3.05 - 3.20	3.12	$0.392 \pm 0.007$
3.20 - 3.35	3.27	$0.400 \pm 0.007$
3.35 - 3.50	3.42	$0.410 \pm 0.008$
3.50 - 3.65	3.57	$0.366 \pm 0.007$
3.65 - 4.00	3.82	$0.430 \pm 0.006$
4.00 - 5.00	4.41	$0.483 \pm 0.008$

Table 2:  $f_{A_b^0}/f_d$  in bins of  $\eta$  of the  $b$  hadron. The uncertainties include the statistical uncertainty on the measured yields. The systematic uncertainty and the uncertainties originating from the scale factor  $\mathcal{S}$  are not included. The statistical uncertainty on the measured efficiency is treated as a systematic uncertainty.

- The systematic uncertainties on the measurement of  $\mathcal{R}$  are treated as correlated between the bins. Tables 3 and 4 list all sources of systematic uncertainty on  $f_{A_b^0}/f_d$  in bins of  $p_T$  and  $\eta$  bins, respectively, related to the measurement of  $\mathcal{R}$ . Also the systematic uncertainty due to the simulated sample size is given in these tables. This uncertainty is uncorrelated between the bins.
- The relative uncertainty on  $f_{A_b^0}/f_d$  originating from the uncertainty on the scale factor  $\mathcal{S}$  is  ${}_{-8.1}^{+7.7}\%$ . This uncertainty includes both the statistical and the systematic uncertainty, and is fully correlated between the bins.

Table 3: Different sources of systematic uncertainty on  $f_{A_b^0}/f_d$  in bins of the  $p_T$  of the  $b$  hadron. The uncertainties listed in this table originate from the measurement of  $\mathcal{R}$ .

$p_T$ [GeV/c] of the $b$ hadron	Uncertainty									
	1.5 - 3.6	3.6 - 4.5	4.5 - 5.3	5.3 - 6.0	6.0 - 6.5	6.5 - 7.0	7.0 - 7.5	7.5 - 8.0	8.0 - 8.5	8.5 - 9.0
Fitmodel: signal shape										
$\alpha_1 - 10\%$	0.30 %	0.14 %	0.07 %	0.23 %	0.02 %	0.15 %	0.13 %	0.18 %	0.14 %	0.22 %
$\alpha_1 + 10\%$	-0.22 %	-0.05 %	0.02 %	-0.13 %	0.06 %	-0.01 %	-0.02 %	-0.14 %	0.04 %	-0.10 %
$\alpha_2 - 10\%$	0.03 %	-0.02 %	0.03 %	0.03 %	-0.04 %	0.07 %	0.06 %	-0.02 %	0.04 %	-0.00 %
$\alpha_2 + 10\%$	-0.01 %	0.02 %	-0.01 %	0.01 %	0.05 %	-0.02 %	-0.03 %	-0.04 %	0.01 %	0.01 %
$n_1 - 10\%$	0.05 %	0.00 %	-0.02 %	0.02 %	-0.04 %	-0.00 %	0.00 %	-0.02 %	-0.01 %	0.01 %
$n_1 + 10\%$	-0.03 %	0.03 %	0.05 %	0.03 %	0.05 %	0.06 %	0.04 %	-0.03 %	0.07 %	0.00 %
$n_2 - 20\%$	0.02 %	0.00 %	0.02 %	0.02 %	-0.00 %	0.04 %	0.02 %	-0.02 %	0.02 %	-0.00 %
$n_2 + 20\%$	0.00 %	0.02 %	0.00 %	0.02 %	0.01 %	0.02 %	0.01 %	-0.03 %	0.04 %	0.01 %
Double Gauss	-0.09 %	0.03 %	-0.07 %	0.15 %	-0.03 %	0.13 %	0.03 %	0.06 %	0.15 %	0.08 %
Fitmodel: background shapes										
comb +50% - -50%	0.14 %	0.00 %	0.16 %	0.11 %	0.15 %	0.20 %	0.08 %	0.09 %	-0.01 %	0.01 %
comb -50% - +50%	0.73 %	0.33 %	0.39 %	0.47 %	0.09 %	0.24 %	0.22 %	0.03 %	0.13 %	0.02 %
$B^0 \rightarrow D^* \pi^+$ shape	0.19 %	0.08 %	0.01 %	0.11 %	0.05 %	-0.02 %	0.09 %	-0.07 %	0.07 %	0.06 %
part reco shape in $A_b^0 \rightarrow A_c^+ \pi^-$	0.13 %	0.12 %	0.16 %	0.01 %	0.03 %	0.15 %	0.15 %	0.02 %	0.14 %	-0.07 %
$B^0 \rightarrow D^- \pi^+$ shape fix in $A_b^0 \rightarrow A_c^+ \pi^-$	0.04 %	-0.00 %	0.03 %	-0.10 %	-0.11 %	0.03 %	0.04 %	-0.06 %	-0.06 %	-0.09 %
Charmless background	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %
Efficiencies										
PID	0.74 %	-3.47 %	-2.02 %	1.61 %	-0.99 %	-2.25 %	0.78 %	-2.36 %	-2.89 %	0.43 %
Trigger	$\pm 0.2\%$	$\pm 0.2\%$	$\pm 0.3\%$	$\pm 0.3\%$	$\pm 0.4\%$	$\pm 0.3\%$	$\pm 0.4\%$	$\pm 0.4\%$	$\pm 0.4\%$	$\pm 0.5\%$
BDTmin	-5.854 %	-1.441 %	-1.640 %	-2.928 %	-1.887 %	-1.321 %	-2.407 %	-1.024 %	-4.563 %	-1.799 %
BDTplus	5.854 %	1.441 %	1.640 %	2.928 %	1.887 %	1.321 %	2.407 %	1.024 %	4.563 %	1.799 %
MC statistics	$\pm 5.25\%$	$\pm 5.45\%$	$\pm 4.90\%$	$\pm 4.68\%$	$\pm 5.16\%$	$\pm 4.74\%$	$\pm 4.60\%$	$\pm 5.15\%$	$\pm 5.05\%$	$\pm 4.78\%$
Fitmodel: signal shape										
$\alpha_1 - 10\%$	0.17 %	0.19 %	0.31 %	0.27 %	0.40 %	0.61 %	0.40 %	0.57 %	0.34 %	0.28 %
$\alpha_1 + 10\%$	0.01 %	0.06 %	-0.16 %	-0.11 %	-0.15 %	-0.43 %	-0.20 %	-0.22 %	-0.16 %	-0.15 %
$\alpha_2 - 10\%$	0.05 %	0.05 %	-0.04 %	-0.05 %	0.01 %	-0.10 %	-0.02 %	-0.02 %	-0.06 %	0.06 %
$\alpha_2 + 10\%$	0.03 %	0.01 %	0.00 %	-0.02 %	0.01 %	0.06 %	-0.04 %	0.07 %	-0.03 %	-0.09 %
$n_1 - 10\%$	0.03 %	-0.00 %	0.01 %	-0.01 %	0.05 %	0.10 %	0.03 %	0.10 %	-0.03 %	-0.05 %
$n_1 + 10\%$	0.06 %	0.08 %	-0.04 %	-0.04 %	-0.01 %	-0.10 %	-0.04 %	-0.01 %	-0.04 %	-0.01 %
$n_2 - 20\%$	0.04 %	0.03 %	-0.02 %	-0.02 %	0.01 %	-0.04 %	-0.02 %	0.02 %	-0.04 %	-0.00 %
$n_2 + 20\%$	0.04 %	0.03 %	-0.01 %	-0.03 %	0.01 %	0.02 %	-0.02 %	0.04 %	-0.04 %	-0.06 %
Double Gauss	-0.02 %	0.09 %	-0.03 %	-0.04 %	0.04 %	-0.02 %	0.15 %	0.13 %	0.25 %	0.30 %
Fitmodel: background shapes										
comb +50% - -50%	0.53 %	0.39 %	0.26 %	0.02 %	0.06 %	0.02 %	0.07 %	0.09 %	0.00 %	-0.57 %
comb -50% - +50%	1.93 %	1.25 %	0.49 %	0.31 %	0.05 %	0.02 %	-0.01 %	0.04 %	0.14 %	-0.01 %
$B^0 \rightarrow D^* \pi^+$ shape	-0.08 %	-0.07 %	0.08 %	0.01 %	0.09 %	0.02 %	-0.07 %	-0.04 %	-0.07 %	0.40 %
part reco shape in $A_b^0 \rightarrow A_c^+ \pi^-$	0.31 %	0.24 %	0.51 %	0.31 %	-0.14 %	0.12 %	0.55 %	1.14 %	0.98 %	2.22 %
$B^0 \rightarrow D^- \pi^+$ shape fix in $A_b^0 \rightarrow A_c^+ \pi^-$	0.15 %	0.11 %	0.27 %	0.08 %	-0.17 %	-0.15 %	0.09 %	0.58 %	-0.18 %	1.33 %
Charmless background	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %
Efficiencies										
PID	-0.62 %	-4.66 %	0.35 %	0.21 %	-4.45 %	-3.41 %	-1.78 %	-2.75 %	-0.53 %	-1.77 %
Trigger	$\pm 0.4\%$	$\pm 0.4\%$	$\pm 0.4\%$	$\pm 0.4\%$	$\pm 0.4\%$	$\pm 0.4\%$	$\pm 0.3\%$	$\pm 0.3\%$	$\pm 0.2\%$	$\pm 0.1\%$
BDTmin	0.615 %	-2.284 %	2.084 %	-0.283 %	-1.824 %	0.867 %	0.660 %	1.085 %	-0.861 %	0.242 %
BDTplus	-0.615 %	2.284 %	-2.084 %	0.283 %	1.824 %	-0.867 %	-0.660 %	-1.085 %	0.861 %	-0.242 %
MC statistics	$\pm 4.91\%$	$\pm 5.00\%$	$\pm 4.36\%$	$\pm 4.08\%$	$\pm 4.87\%$	$\pm 5.28\%$	$\pm 3.92\%$	$\pm 4.40\%$	$\pm 3.75\%$	$\pm 4.27\%$

Table 4: Different sources of systematic uncertainty on  $f_{A_0^0}/f_d$  in bins of the  $b$  hadron. The uncertainties listed in this table originate from the measurement of  $\mathcal{R}$ .

$\eta$ of the $b$ hadron	Uncertainty									
	2.00 - 2.60	2.60 - 2.75	2.75 - 2.90	2.90 - 3.05	3.05 - 3.20	3.20 - 3.35	3.35 - 3.50	3.50 - 3.65	3.65 - 4.00	4.00 - 5.00
Fitmodel: signal shape										
$\alpha_1 - 10\%$	0.64 %	0.56 %	0.41 %	0.41 %	0.32 %	0.30 %	0.24 %	0.13 %	0.07 %	0.02 %
$\alpha_1 + 10\%$	-0.34 %	-0.34 %	-0.20 %	-0.21 %	-0.08 %	-0.12 %	-0.09 %	-0.03 %	0.00 %	0.03 %
$\alpha_2 - 10\%$	-0.02 %	0.07 %	0.02 %	0.08 %	0.03 %	-0.00 %	0.01 %	-0.02 %	-0.03 %	-0.04 %
$\alpha_2 + 10\%$	0.03 %	-0.07 %	-0.02 %	-0.05 %	0.02 %	0.02 %	-0.02 %	-0.01 %	0.01 %	0.02 %
$n_1 - 10\%$	0.13 %	0.13 %	0.06 %	0.07 %	0.07 %	0.03 %	0.00 %	-0.02 %	-0.04 %	-0.05 %
$n_1 + 10\%$	-0.05 %	-0.09 %	-0.05 %	-0.03 %	0.01 %	-0.01 %	0.00 %	0.00 %	0.03 %	0.03 %
$n_2 - 20\%$	-0.00 %	0.02 %	-0.00 %	0.03 %	0.02 %	0.00 %	0.00 %	-0.02 %	-0.00 %	-0.00 %
$n_2 + 20\%$	0.03 %	-0.01 %	0.00 %	0.00 %	0.02 %	0.01 %	-0.01 %	-0.01 %	-0.01 %	-0.01 %
Double Gauss	0.23 %	0.07 %	-0.02 %	0.01 %	0.06 %	0.09 %	0.03 %	-0.02 %	0.10 %	-0.11 %
Fitmodel: background shapes										
comb +50% - -50%	0.53 %	0.39 %	0.26 %	0.02 %	0.06 %	0.02 %	0.07 %	0.09 %	0.00 %	-0.57 %
comb -50% - +50%	1.93 %	1.25 %	0.49 %	0.31 %	0.05 %	0.02 %	-0.01 %	0.04 %	0.14 %	-0.01 %
$B^0 \rightarrow D^{*-} \pi^+$ shape	-0.02 %	0.03 %	0.02 %	-0.00 %	-0.01 %	0.04 %	0.01 %	0.02 %	0.10 %	0.46 %
part reco shape in $A_b^0 \rightarrow A_c^+ \pi^-$	0.02 %	0.03 %	-0.11 %	0.33 %	-0.02 %	0.02 %	0.26 %	0.35 %	0.16 %	0.12 %
$B^0 \rightarrow D^- \pi^+$ shape fix in $A_b^0 \rightarrow A_c^+ \pi^-$	-0.77 %	-0.32 %	-0.28 %	0.10 %	-0.17 %	-0.22 %	0.12 %	0.12 %	0.05 %	0.02 %
Charmless background	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %	0.4 %
Efficiencies										
PID	-1.74 %	-4.59 %	-2.32 %	-3.03 %	-1.02 %	-1.47 %	-1.36 %	-1.41 %	-0.25 %	3.33 %
Trigger	$\pm 0.4$ %	$\pm 0.3$ %	$\pm 0.4$ %	$\pm 0.4$ %	$\pm 0.4$ %	$\pm 0.3$ %	$\pm 0.3$ %	$\pm 0.3$ %	$\pm 0.3$ %	$\pm 0.3$ %
BDTmin	-0.887 %	-1.027 %	-1.387 %	-1.105 %	-1.223 %	-1.695 %	-1.017 %	-0.531 %	-2.212 %	-2.244 %
BDTplus	0.887 %	1.027 %	1.387 %	1.105 %	1.223 %	1.695 %	1.017 %	0.531 %	2.212 %	2.244 %
MC Statistics	$\pm 2.94$ %	$\pm 3.77$ %	$\pm 3.48$ %	$\pm 3.40$ %	$\pm 3.45$ %	$\pm 3.54$ %	$\pm 3.72$ %	$\pm 3.60$ %	$\pm 2.96$ %	$\pm 3.76$ %

### 1.3 $f_{\Lambda_b^0}/f_d$ comparison

A comparison of the present measurement of  $f_{\Lambda_b^0}/f_d$  to the semileptonic measurement is provided in Fig. 1.

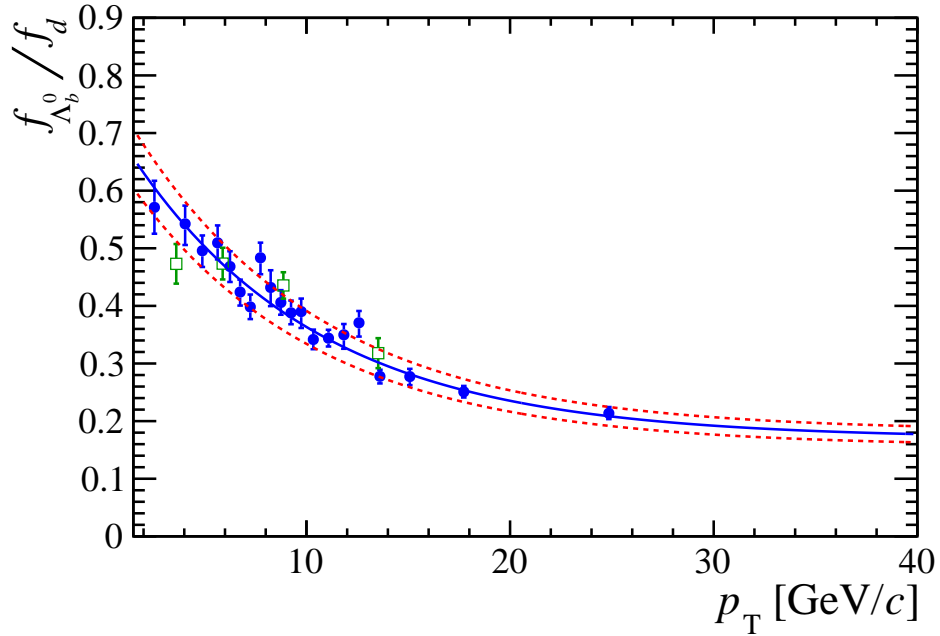


Figure 1: Dependence of  $f_{\Lambda_b^0}/f_d$  on the  $p_T$  of the  $b$  hadron. The green (open square) data points show the semileptonic measurement. Only the statistical uncertainty is included. The blue (solid circle) data points show the hadronic measurement, and include both the statistical and systematic uncertainty. The red lines indicate the uncertainty on the scale of  $f_{\Lambda_b^0}/f_d$  from the semileptonic measurement.