## LHCb-PAPER-2014-051 supplementary material



Figure 1: Decay time distribution as per Fig.4 with pull distribution included.



Figure 2: Mass distributions as per Fig.1 with pull distributions included.



Figure 3: Mass distributions as per Fig.1 on a logarithmic scale, with pull distributions included.



Figure 4: Correction factor between simulated  $D_s^+D_s^-$  and  $D^-D_s^+$  acceptances. This is the correction applied to the  $D^-D_s^+$  data-driven acceptance in Fig. 2(a), green, in order to obtain Fig. 2(b), red.



Figure 5: Profile likelihood of  $\phi_s$  for the  $|\lambda| = 1$  fit (top) and the floated  $|\lambda|$  fit (bottom) in data.



Figure 6: Profile likelihood of  $|\lambda|$  in data.



Figure 7: The raw asymmetry distributions with fits overlaid. The offset is due to a difference in the number of  $\overline{B}^0_s$  and  $B^0_s$  tags, which corresponds to an asymmetry in the tagging efficiency that is, however, consistent with zero. On top is the case where  $|\lambda|$  is a free parameter. The flavour tagging calibration has been applied to the data, rather than as part of the fit as is the case in the fits to extract  $\phi_s$ .



Figure 8: Calibrated wrong-tag *sPlot* distributions in data. The three tagging categories are shown: Candidates with an opposide-side tag only are shown in red, while candidates with a neural-net same-side kaon tagger only are shown in blue. Candidates with both OS and SSK tags have a combined wrong-tag probability as shown in black.



Figure 9: Inclusive calibrated wrong-tag *sPlot* distributions in data. The two tagging categories are shown: All candidates with an opposide-side tag are shown in red, while candidates with a neural-net same-side kaon tag are shown in blue.

Table 1: Inclusive performance of the tagging algorithms used in this analysis, post calibration. The tagging values are determined for events where this tagger makes a decision inclusively, *i.e.*: whether or not the other tagger makes a decision.

	OS Cut-based	SSK Neural-net
Tagging efficiency, $\epsilon$	$(39.18 \pm 0.85)\%$	$(70.53 \pm 0.80)\%$
Effective wrong-tag prob., $\omega_{\rm eff}$	$0.3508 \pm 0.0015 \pm 0.0037$	$0.4084 \pm 0.0045 \pm 0.0035$
Effective tagging power $\epsilon D_{\text{eff}}^2$	$(3.49 \pm 0.10 \pm 0.17)\%$	$(2.37 \pm 0.23 \pm 0.18)\%$
Combined $\epsilon D_{\text{eff}}^2$	$(5.33 \pm 0.18 \pm 0.17)\%$	

Table 2: Exclusive performance of the tagging algorithms used in this analysis, post calibration. The exclusive tagging values are determined for events where only this tagger makes a decision. The Overlap values are determined for events where both tagging algorithms make a decision.

	OS Cut-based	SSK Neural-net	
Excl. tagging eff., $\epsilon$	$(10.66 \pm 0.54)\%$	$(40.02 \pm 0.86)\%$	
Excl. effective wrong-tag prob., $\omega_{\rm eff}$	$0.3405 \pm 0.0016 \pm 0.0039$	$0.4057 \pm 0.0046 \pm 0.0036$	
Excl. effective tagging power $\epsilon D_{\text{eff}}^2$	$(1.08 \pm 0.06 \pm 0.05)\%$	$(1.42 \pm 0.46 \pm 0.36)\%$	
Overlap $\epsilon$	$(26.51 \pm 0.77)\%$		
Overlap $\omega_{\text{eff}}$	$0.3367 \pm 0.0016 \pm 0.0033$		
Overlap $\epsilon D_{\text{eff}}^2$	$(2.83 \pm 0.10 \pm 0.11)\%$		
Combined $\epsilon D_{\text{eff}}^2$	$(5.33 \pm 0.1)$	$8 \pm 0.17)\%$	



Figure 10: Diagrams pertinent to  $\bar{B}^0_s \rightarrow D^+_s D^-_s$ . Left:  $\bar{B}^0_s - B^0_s$  mixing. Centre:  $\bar{B}^0_s \rightarrow D^+_s D^-_s$  tree, Right:  $\bar{B}^0_s \rightarrow D^+_s D^-_s$  penguin.



Figure 11: Effective resolution determination in simulated signal candidates. A triple-Gaussian is overlaid. The effective resolution is the fractional weighted quadrature sum of the widths of the three Gaussians.



Figure 12: Effective resolution as a function of the per-event decay time error. A linear  $\chi^2$  fit is overlaid, in which both horizontal and vertical uncertainties are taken into account.