## Supplementary material for LHCb-PAPER-2015-049

We thank B.F.L. Ward for providing MC@NLO [1] + HERWIG++ [2] and MC@NLO + HERWIRI [3] predictions.

- The differential Z boson production cross-section as a function of  $p_{T,Z}$ ,  $\phi_{\eta}^*$  and  $\eta^{\mu}$  is shown in Figs. 1, 2, 3, 4 and 5.
- The comparison between the present measurements with those of Ref. [4] is shown in Figs. 6 and 7.
- The differential Z boson production cross-section at  $\sqrt{s} = 7$  TeV as a function of  $\eta^{\mu}$ , and the differential  $W^{\pm}$  to Z ratios are shown in Figs. 8 and 9.
- The energy evolution of the  $W^+$ ,  $W^-$  and Z boson production cross-section is shown in Fig. 10.



Figure 1: Normalised differential cross-section as a function of  $p_{T,Z}$  on (top) logarithmic and (bottom) linear scales. The measurements are compared to the predictions of POWHEG + HERWIG and POWHEG + PYTHIA.



Figure 2: Normalised differential cross-section as a function of  $\phi_{\eta}^*$  on (top) logarithmic and (bottom) linear scales. The measurements are compared to the predictions of POWHEG + HERWIG and POWHEG + PYTHIA.



Figure 3: Normalised differential cross-section as a function of  $p_{T,Z}$  on (top) logarithmic and (bottom) linear scales. The measurements are compared to MC@NLO + HERWIG (HW) and MC@NLO + HERWIRI (HERWIRI). HERWIG is configured with two choices of the root mean-square-deviation of the intrinsic  $k_T$  distribution, 0 and 2.2 GeV/c.



Figure 4: Normalised differential cross-section as a function of  $\phi_{\eta}^*$  on (top) logarithmic and (bottom) linear scales. The measurements are compared to MC@NLO + HERWIG (HW) and MC@NLO + HERWIRI (HERWIRI). HERWIG is configured with two choices of the root mean-square-deviation of the intrinsic  $k_T$  distribution, 0 and 2.2 GeV/c.



Figure 5: Differential Z cross-section in bins of muon pseudorapidity. Measurements, represented as bands, are compared to (markers, displaced horizontally for presentation) NNLO predictions with different parameterisations of the PDFs.



Figure 6: Differential Z boson production cross-section as a function of (top)  $y_Z$  and (bottom)  $\phi_{\eta}^*$ .



Figure 7: Summary of the Z boson cross-section.



Figure 8: Differential Z cross-section in bins of muon pseudorapidity at 7 TeV. Measurements, represented as bands, are compared to (markers, displaced horizontally for presentation) NNLO predictions with different parameterisations of the PDFs.



Figure 9: Differential  $W^+$  and  $W^-$  to Z cross-section ratios in bins of muon pseudorapidity at  $\sqrt{s} = 7$  TeV. Measurements, represented as bands, are compared to (markers, displaced horizontally for presentation) NNLO predictions with different parameterisations of the PDFs.



Figure 10: Summary of the W and Z cross-section as a function of the centre-of-mass energy. Measurements, represented as markers, are compared to NNLO predictions calculated with the MSTW08 PDF set.

## References

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