## Supplemental material for LHCb-PAPER-2016-022

## Diagrams of the processes

The main leading order diagrams contributing to the phase space of the  $B_c^+$  decays to the  $K^+K^-\pi^+$  final state are shown in Fig. 1.



Figure 1: Different processes populating the phase space of the  $B_c^+ \to K^+ K^- \pi^+$  decay: (a) pure annihilation, (b)  $B_c^+ \to D^0(\to K^-\pi^+)K^+$ , (c)  $B_c^+ \to B_s^0(\to K^+K^-)\pi^+$ ,  $B^0(\to \pi^+K^-)K^+$  and (d) charmonium  $B_c^+ \to [c\bar{c}](\to K^-K^+)\pi^+$  mode.

## Fits to the regions $B_c^+ \to D^0(\to K^-\pi^+)K^+$ and $B_c^+ \to B_s^0(\to K^+K^-)\pi^+$

The results of the simultaneous fits for  $B_c^+ \to D^0(\to K^-\pi^+)K^+$  and  $B_c^+ \to B_s^0(\to K^+K^-)\pi^+$  are shown in Fig. 2.



Figure 2: Projection of the fit to the to the  $K^+K^-\pi^+$  invariant mass for the (left)  $D^0 \to K^-\pi^+$ and (right)  $B_s^0 \to K^+K^-$  regions, in the bins of BDT output (top)  $0.04 < \mathcal{O}_{BDT} < 0.12$ , (middle)  $0.12 < \mathcal{O}_{BDT} < 0.18$  and (bottom)  $\mathcal{O}_{BDT} > 0.18$ . The contributions are indicated according to the same scheme as in the first figure of the article.

## *p*-value scans

The *p*-value scans for the different  $R \equiv \frac{\sigma(B_c^+)}{\sigma(B^+)} \times \mathcal{B}$  measurements are shown in Figs. 3 and 4.



Figure 3: The *p*-value associated to the profile likelihoods as a function of the observables for (left) annihilation signal and (right)  $B_c^+ \rightarrow \chi_{c0}\pi^+$ . The horizontal solid red, dashed blue and dotted blue lines represented the values 32%, 10% and 5% defining the 68%, 90% and 95% confidence intervals, respectively.



Figure 4: The *p*-value associated to the profile likelihoods as a function of the observables for (left)  $B_c^+ \to D^0 K^+$  and (right)  $B_c^+ \to B_s^0 \pi^+$ . The horizontal dashed blue and dotted blue lines represented the values 10% and 5% defining the 90% and 95% confidence limits, respectively.