

# 1 Supplementary material for LHCb-PAPER-2020-033

3 The  $m(K^+K^-)$  shape of  $B_s^0$  tail leaking into  $B^0$  signal region is extracted from an unbinned  
 4 maximum-likelihood fit to the  $B_s^0 \rightarrow J/\psi \phi$  simulation, as shown in Fig. 1. The  $m(K^+K^-)$   
 5 shape of  $\Lambda_b^0 \rightarrow J/\psi p K^-$  background is found to be independent on  $m(J/\psi K^+K^-)$  in  
 6 simulation, as shown in Fig. 2. The  $m(K^+K^-)$  shape of combinatorial background has  
 7 been checked to be compatible in different  $J/\psi K^+K^-$  mass regions and with different  
 8 BDT requirements, as shown in Fig. 3.

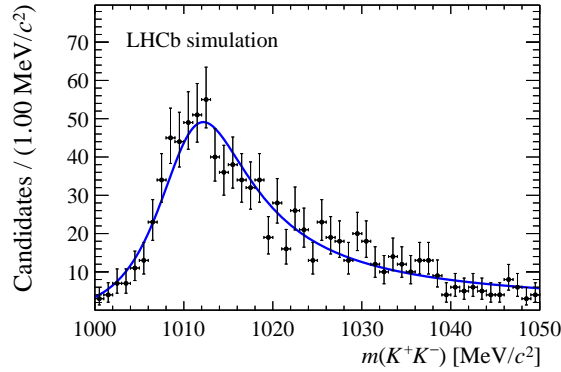


Figure 1: Distribution of  $m(K^+K^-)$  in the  $B^0$  region from a  $B_s^0 \rightarrow J/\psi \phi$  simulation sample, superimposed by a fit to the simulation.

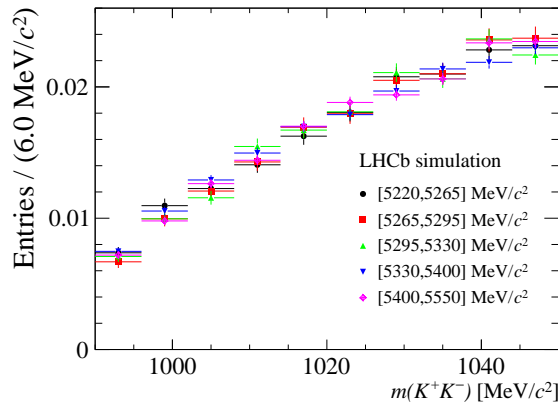


Figure 2: Distributions of the invariant mass  $m(K^+K^-)$  in different  $m(J/\psi K^+K^-)$  intervals with boundaries at 5220, 5265, 5295, 5330, 5400 and 5550  $\text{MeV}/c^2$ . They are obtained using simulated  $\Lambda_b^0 \rightarrow J/\psi p K^-$  decays and normalised to unity.

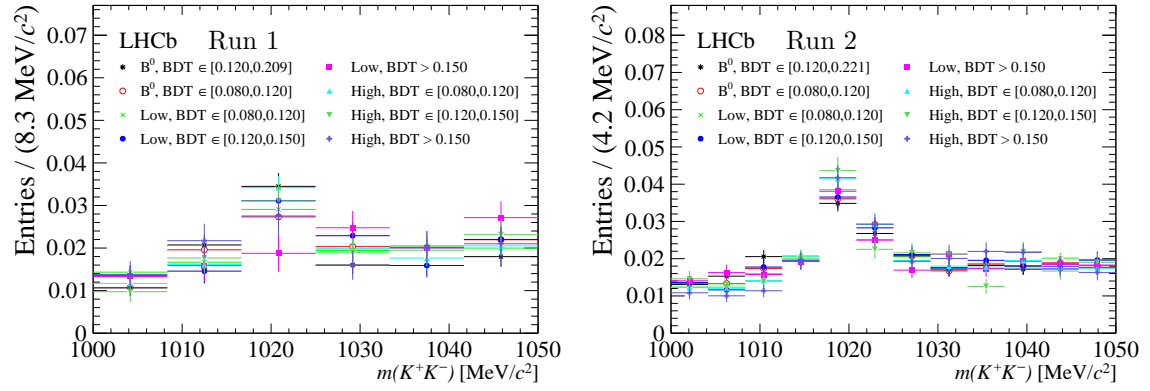


Figure 3: Distributions of the invariant mass  $m(K^+K^-)$  in low mass sideband 5220–5250  $\text{MeV}/c^2$ ,  $B^0$  signal region and high mass sideband 5520–5550  $\text{MeV}/c^2$  with different BDT requirements. They are normalised to unity. The left figure is for Run 1 and the right figure is for Run 2. The  $\Lambda_b^0 \rightarrow J/\psi p K^-$  and  $B_s^0 \rightarrow J/\psi \phi$  contributions are subtracted by injecting simulated events with negative weights.