¹ Supplementary material for LHCb-PAPER-2020-034

² This appendix contains supplementary material that will be posted on the public CDS

 $_{3}$ record but will not appear in the paper. Figure 1 shows a comparison of the spectrum of

 $_{4}$ D_{s}^{+} mesons between theory and experiment. Figure 2 shows several mass projections in

the low $K^+\pi^-$ mass region with the result of the amplitude fit overlaid. Figure 3 shows

6 the amplitude fit result for the model without the $D_{s0}(2590)^+$ state.



Figure 1: Comparison of the observed D_s^+ states from Ref. [1] (labelled with coloured lines) with predictions from Ref. [2] (black lines). Breit–Wigner masses are used for all cases except the $D_{s0}(2590)^+$ state, for which the pole mass reported in this analysis is used. The two dashed gray lines denote the DK and D^*K thresholds. Spectroscopic identification is made in terms of the quantum numbers $n^{2S+1}L_J$ of the constituent quark model where possible, although alternative explanations are possible in some cases. The spin-parity J^P of the $D_{sJ}(3040)^+$ state is not yet determined, but it appears likely to be a member of the 2P set of states. The $D_{s0}(2590)^+$ state, labelled by the red line, is identified as the radial excitation of the pseudoscalar D_s^+ ground-state meson.



Figure 2: Mass projections of (a) D^-K^+ , (b) $D^-K^+\pi^-$ and (c) $D^+D^-\pi^-$ systems. Data points are shown in black with the background subtracted statistically using the *sPlot* method [3]. Results of the fit with the $D_{s0}(2590)^+$ ($J^P = 0^-$) model are overlaid as a solid red histogram, and individual contribution are shown as a dotted histogram. No signature of the charm-strange states, $X_0(2900)$ and $X_1(2900)$ [4,5], is seen in the D^-K^+ mass.



Figure 3: Distributions of (a) $m(D^+K^+\pi^-)$, (b) $m(K^+\pi^-)$, (c) $m(D^+D^-)$, (d) $m(D^+\pi^-)$ and (e) $\cos\theta_{D_s^+}$ for the null hypothesis. Data points are shown in black with the combinatorial background subtracted statistically using the *sPlot* method [3]. Fit results are overlaid as a solid red histogram, and each contribution is shown as a dotted histogram. In the absence of the $D_{s0}(2590)^+$ component the fit cannot describe the peak in $D^+K^+\pi^-$ mass, and also fails to describe associated structures at low $m_{D^+\pi^-}$ and high $m_{D^+D^-}$.

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